



دانشگاه کردستان  
University of Kurdistan  
زانکۆی کوردستان

**Department of Computer and IT Engineering  
University of Kurdistan**

**Complex Networks**

**Introduction**

**By: Dr. Alireza Abdollahpouri**

# Course Info

---

## ➤ Instructor

**Dr. Alireza Abdollahpouri**

**Emails:** [abdollahpouri@gmail.com](mailto:abdollahpouri@gmail.com)

## ➤ Course Web Page

<http://eng.uok.ac.ir/abdollahpouri/CN.html>

## ➤ Grading Policy

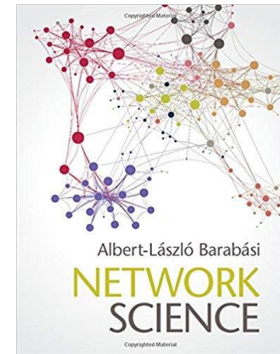
|                            |            |
|----------------------------|------------|
| <b>Homeworks</b>           | <b>20%</b> |
| <b>Project</b>             | <b>20%</b> |
| <b>Final Exam</b>          | <b>55%</b> |
| <b>Class participation</b> | <b>5%</b>  |



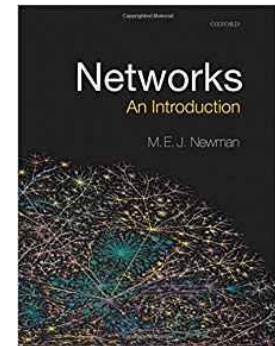
# Teaching Materials – Textbooks

- Barabási, Albert-László. ***“Network Science Book,”*** 2015.

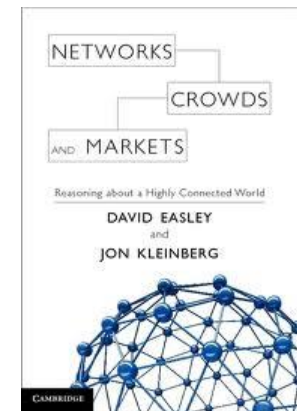
<http://barabasi.com/networksciencebook/>



- Mark Newman, ***Networks: an Introduction***



- David Easley and Jon Kleinberg: ***“Networks Crowds and Markets. Reasoning about a Highly Connected World”***



# Course Overview

---

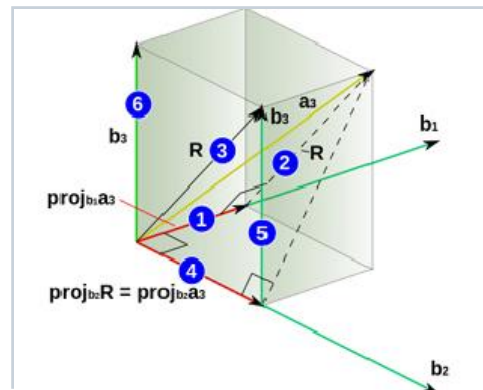
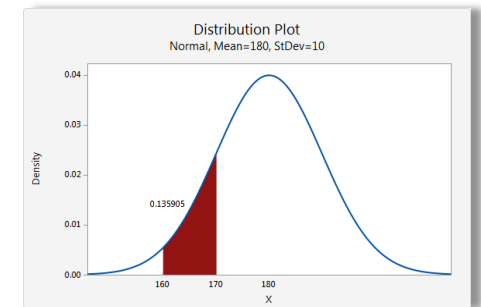
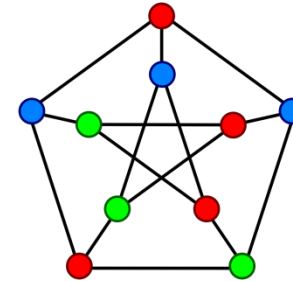
- **Introduction**
- **Graph Theory**
- **Centrality and Ranking**
- **Communities**
- **Network Models**
- **Diffusion models and Influence Maximization**
- **Link Prediction**
- **Network Robustness** (if time allows)



# Course Prerequisites

## ➤ Good background in:

- Algorithms and graph theory
- Probability and statistics
- Linear algebra



## ➤ Programming:

- You should be able to write programs (in Python)



# Some Ground Rules

---

- ❑ Let's make this educational and enjoyable.
- ❑ It's a big size class, I enjoy questions and ideas from the class.
- ❑ Ask questions and raise points.
- ❑ Listen to other people's questions.
- ❑ Be here.
- ❑ Be here on time.



---

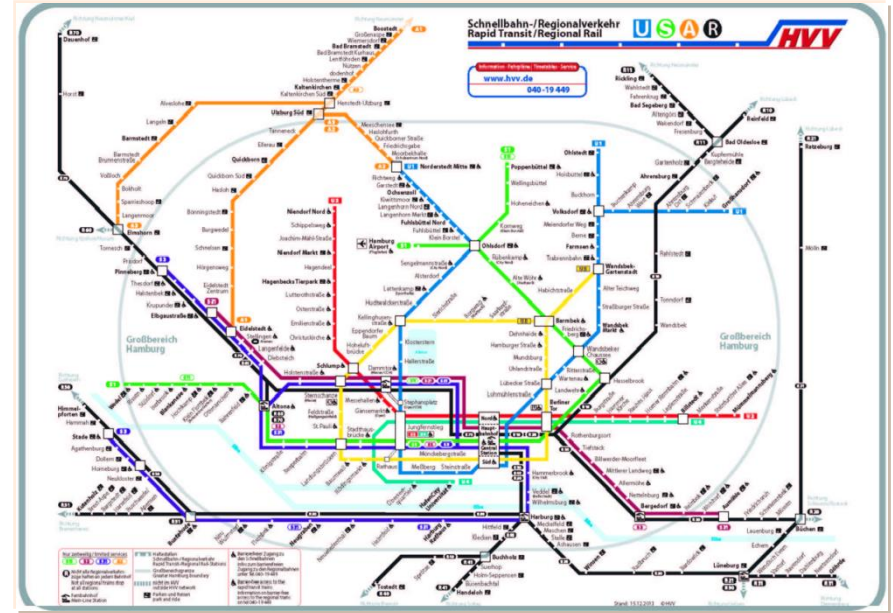
**What do the  
following things  
have in  
common?**



# What do the following things have in common?



World economy

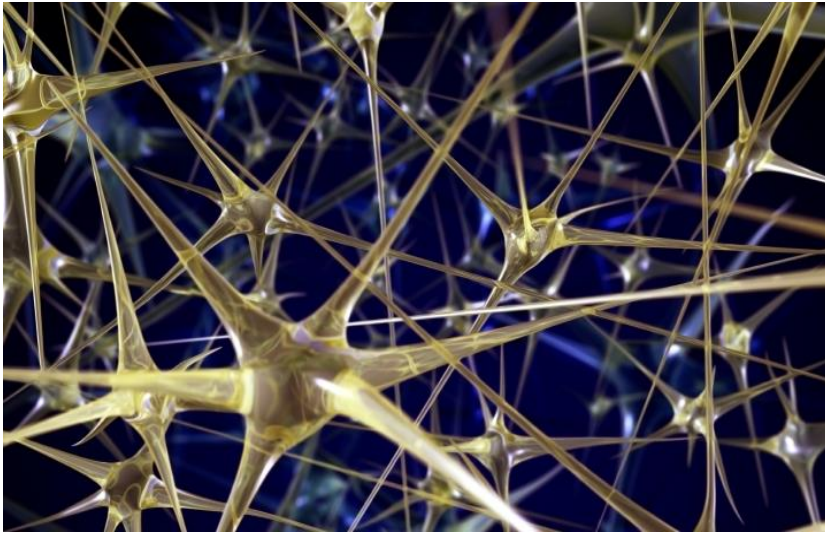


Metro map



# What do the following things have in common?

---



**Human brain**



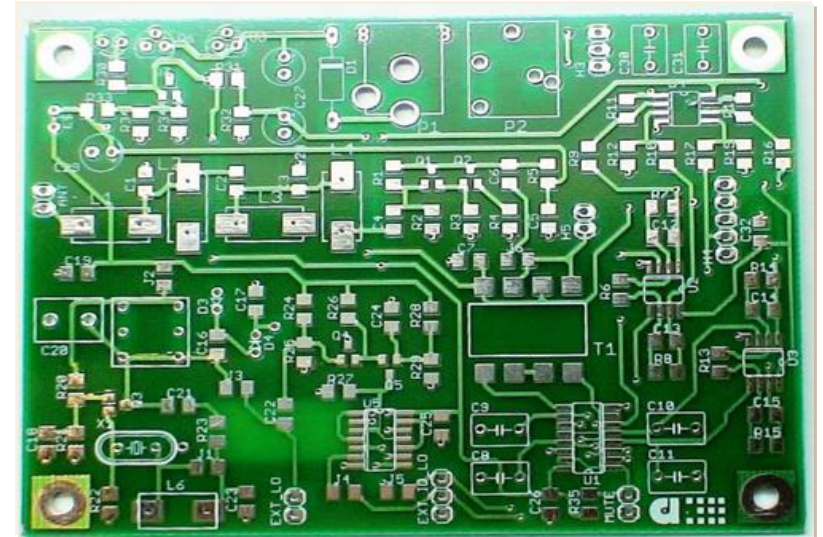
**Family and friends**

# What do the following things have in common?

---



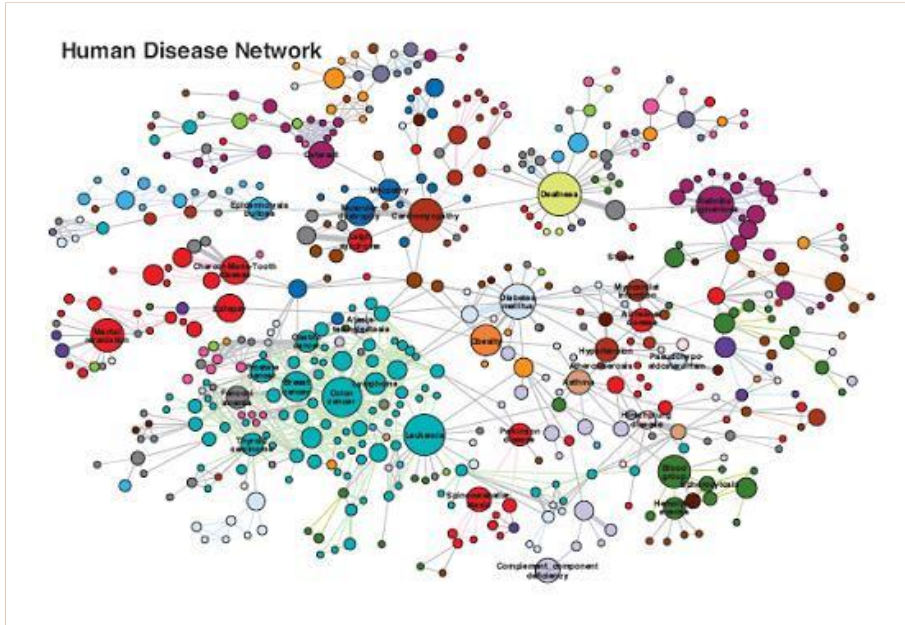
**Power lines**



**Printed circuit board  
(PCB)**

# What do the following things have in common?

---

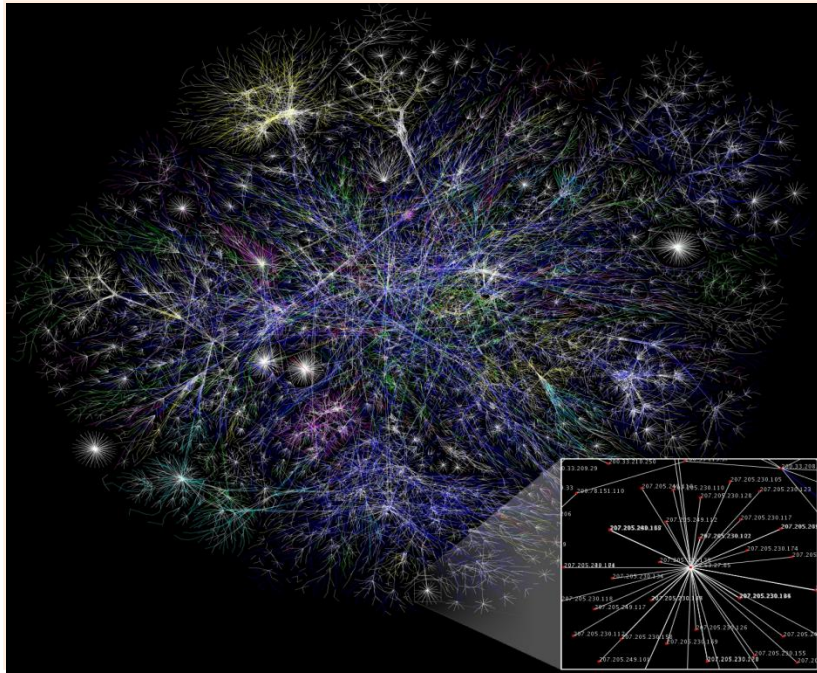


**Human diseases map**

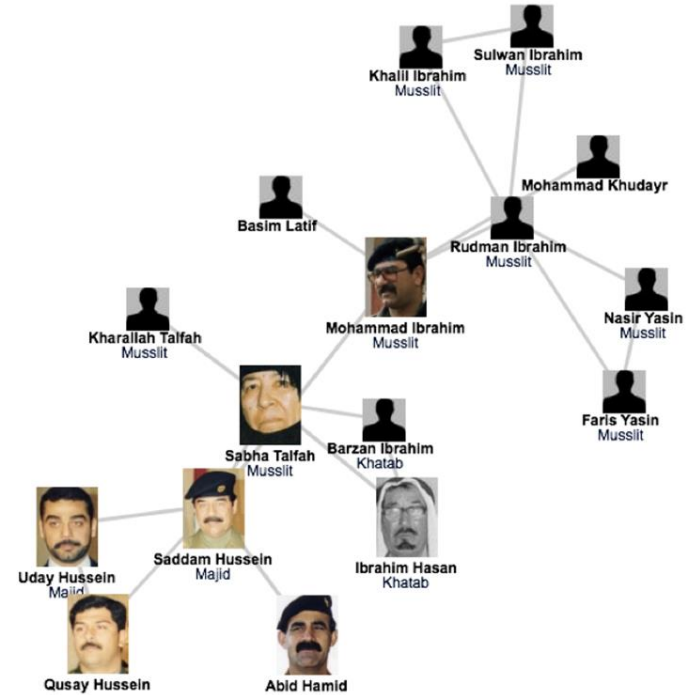


**Transportation highways**

# What do the following things have in common?



Internet



Terrorism

---

**Behind each complex system  
there is a **NETWORK**, that  
defines the interactions  
between the component.**



---

**We will never understand  
these systems unless we  
understand the networks  
behind them!**



# Why Networks?

---

- **Universal language for describing complex data**

Networks from science, nature, and technology are more similar than one would expect

- **Shared vocabulary between fields**

Computer Science, Social science, Physics, Economics, Statistics, Biology



# What is a Network?

---

- A collection of nodes (**vertices**)
- And a collection of edges (**links**) connecting nodes
- A network model treats all nodes and links the same. But there are heterogeneous networks.
- The spatial location of nodes is arbitrary (in visualization)
- Networks are abstractions of connection and relation





# Ubiquity of Networks

Networks appear at all scales

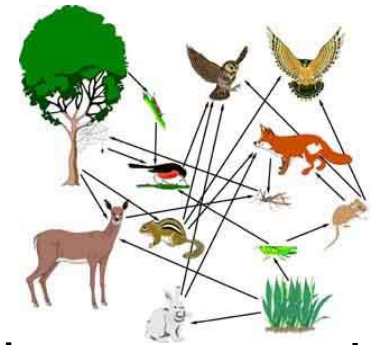
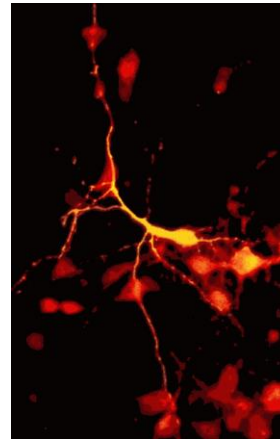
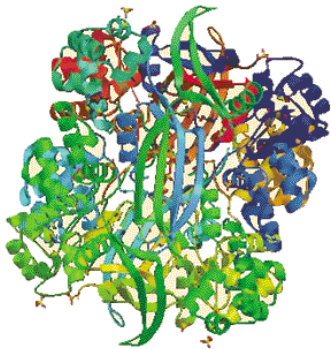
Proteins

Intra-cellular  
signalling

Neuronal  
communication

Social  
contact

Food webs



$10^{-9}$  m

$10^{-6}$  m

$10^{-3}$  m

1 m

$10^3$  m

$10^6$  m

Molecules

Cells

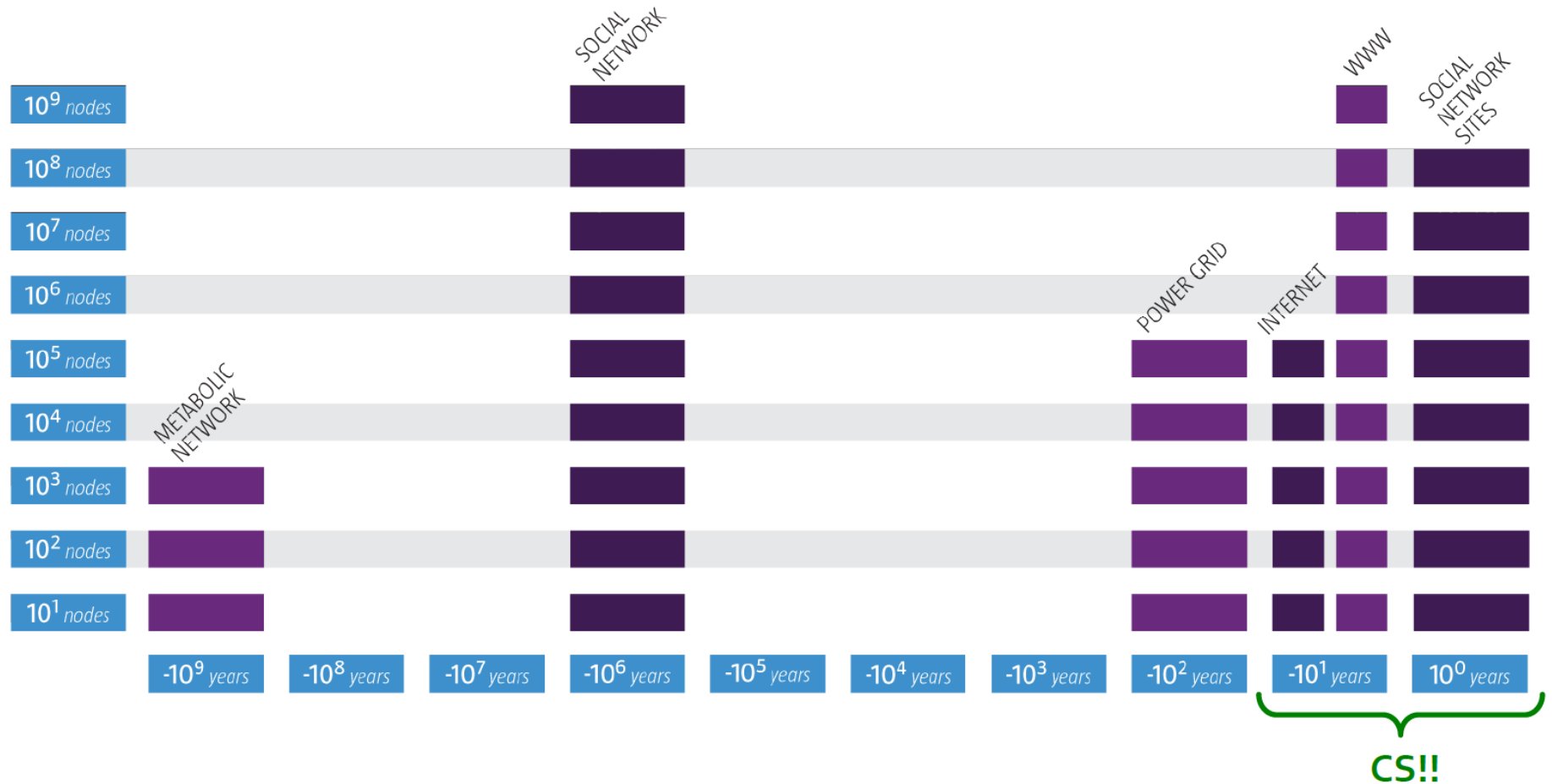
Organisms

Populations

Ecologies



# Age and size of networks




# Many examples of networks

---

- Social Networks**
- Technological Networks**
- Networks of Information**
- Biological Networks**
- And ...**

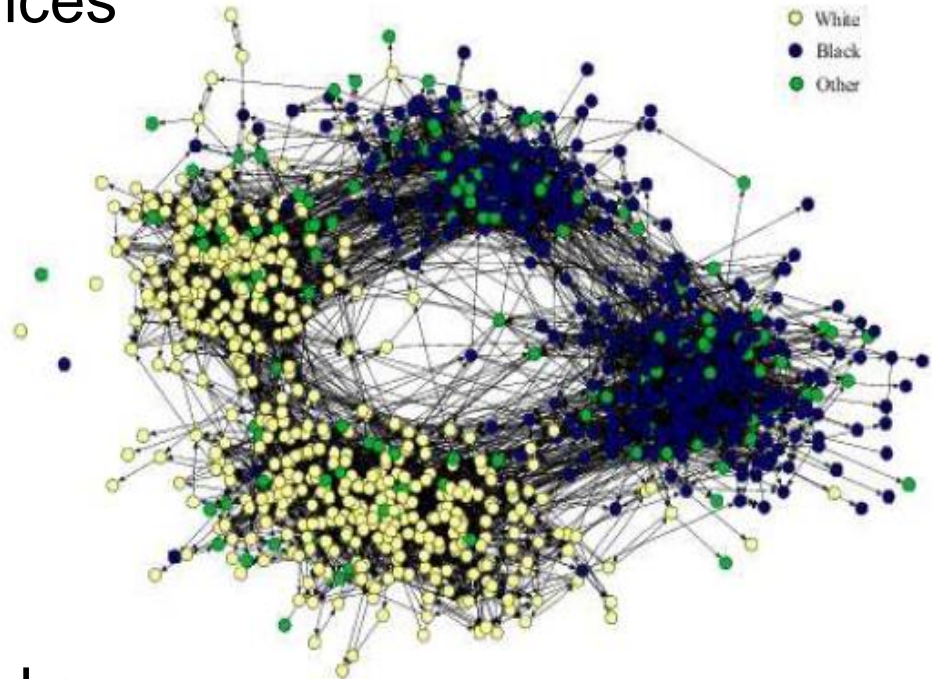


The background features a complex network diagram with numerous nodes (represented by small circles) and connecting lines (edges). The nodes and lines are rendered in various shades of blue and white, creating a sense of depth and connectivity. The overall aesthetic is clean and modern, typical of a digital or technological theme.

# **Social Networks**

# Social Networks

- Links denote a social interaction
  - Networks of acquaintances
  - collaboration networks
    - actor networks
    - co-authorship networks
    - director networks
  - phone-call networks
  - e-mail networks
  - Bluetooth networks
  - home page/blog networks
  - ...



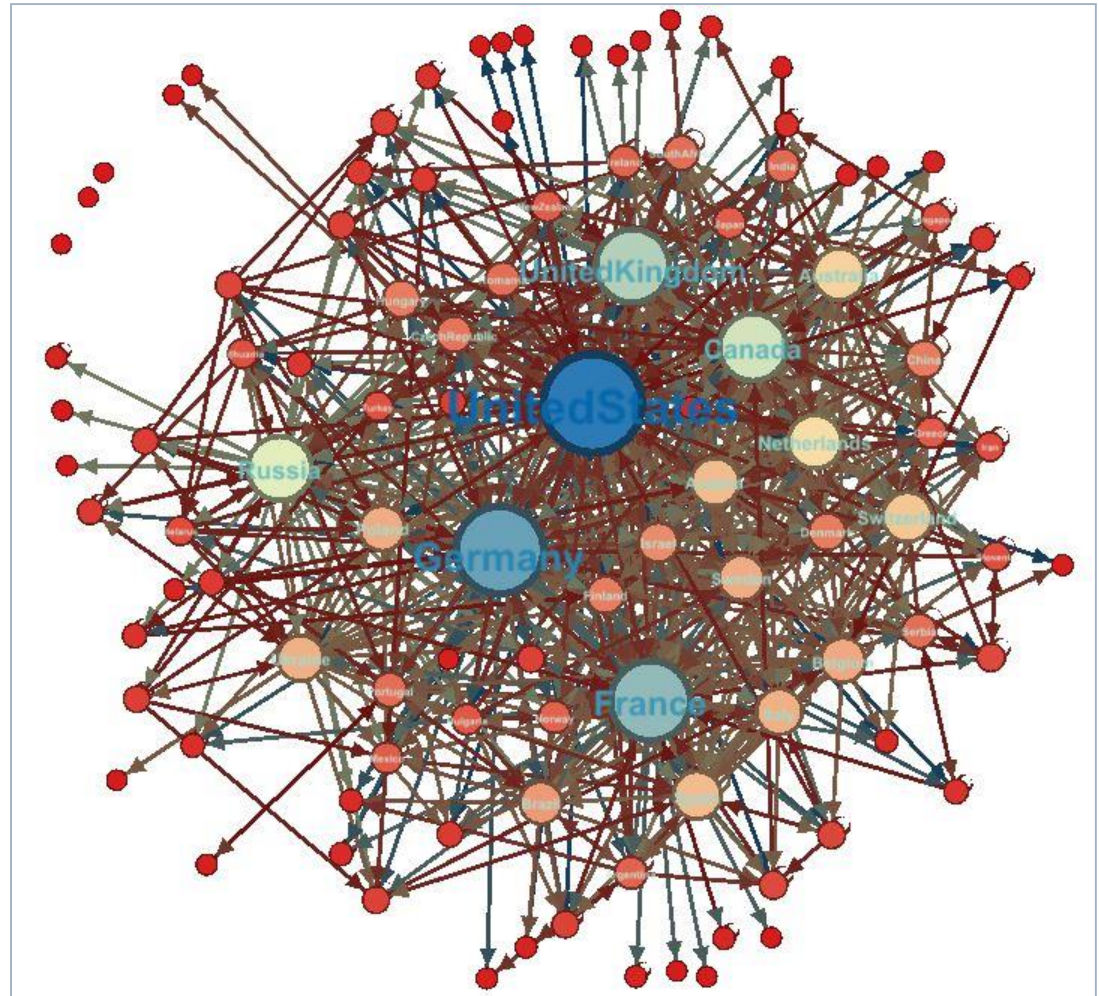
# Academic Network

104 countries

$d = 17.8$

Assortativity = .005  
non-assortative

clustering = .37  
(random = .06)



# Friendship Network

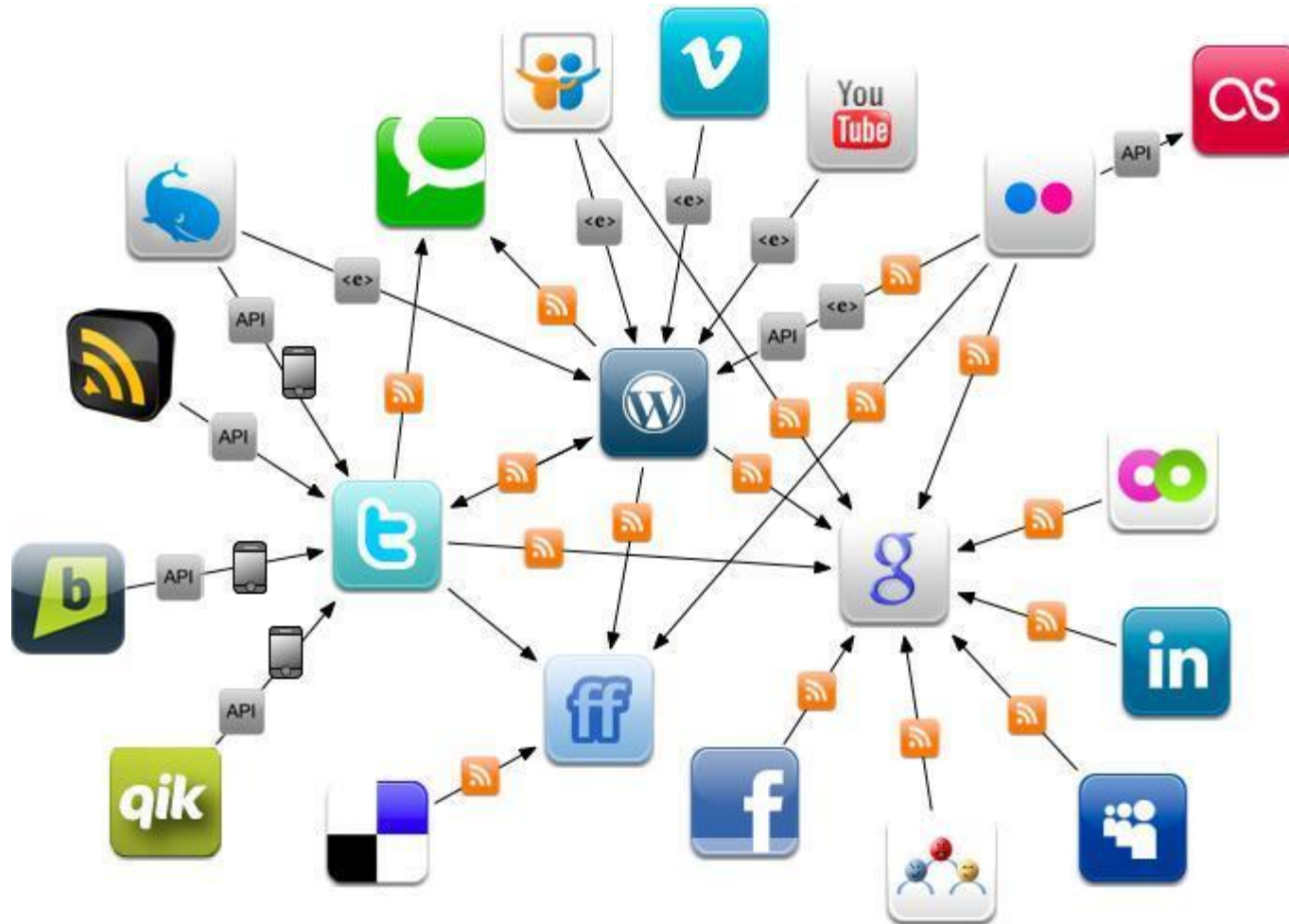
---

- Nodes: all persons in some community
- A link exists between two persons if they are friends.



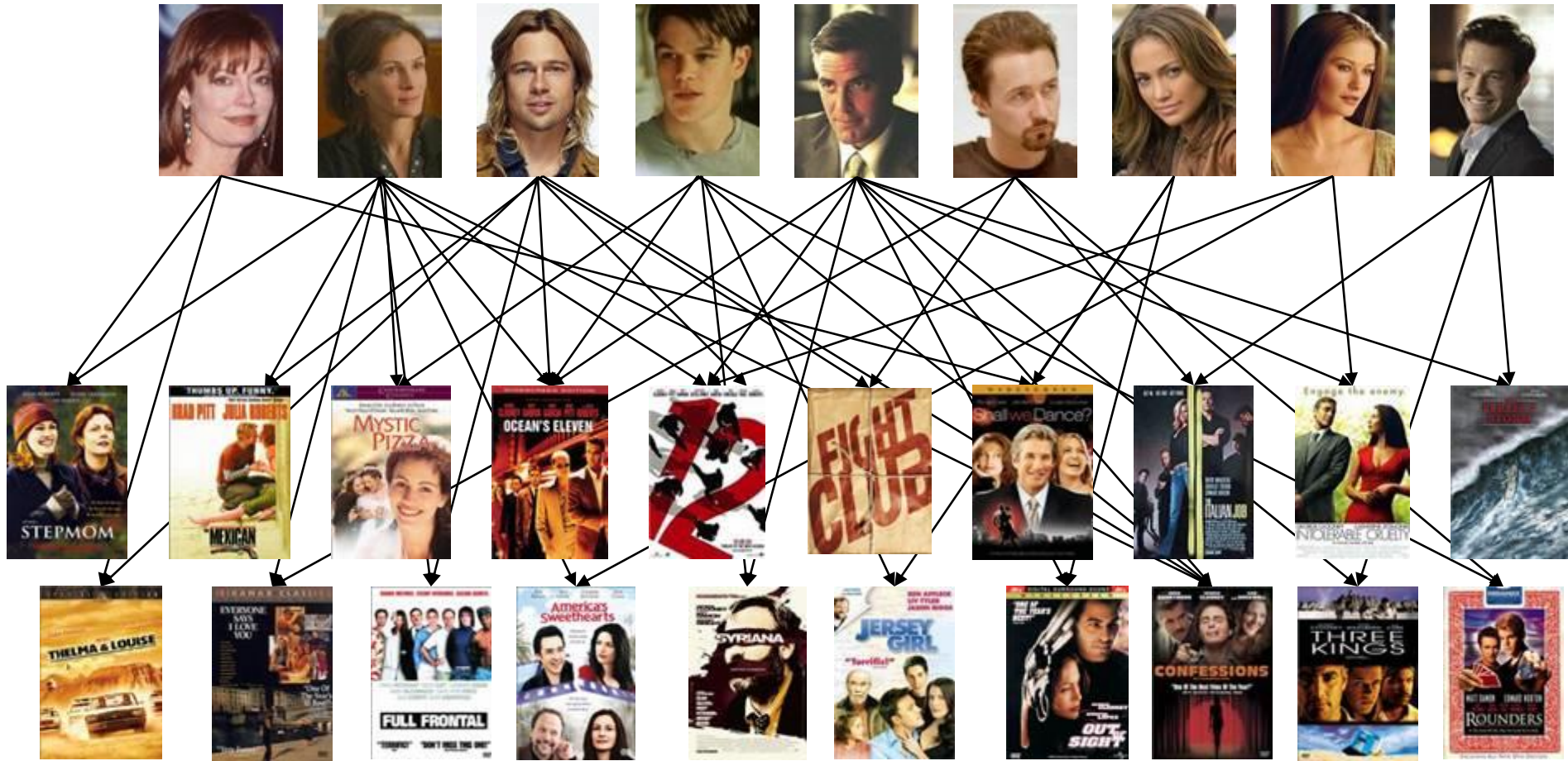
# Online Social Networks

---



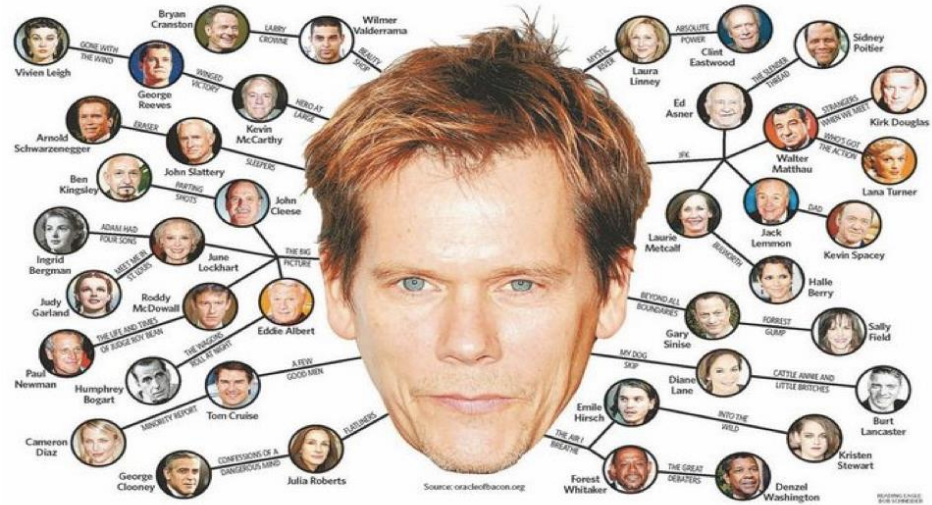


# Network of actor co-starring in movies

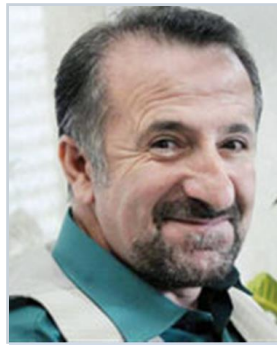
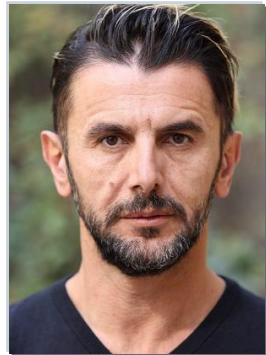


# Actor co-starring Network

- The collaboration graph of film actors
- Six Degrees of Kevin Bacon



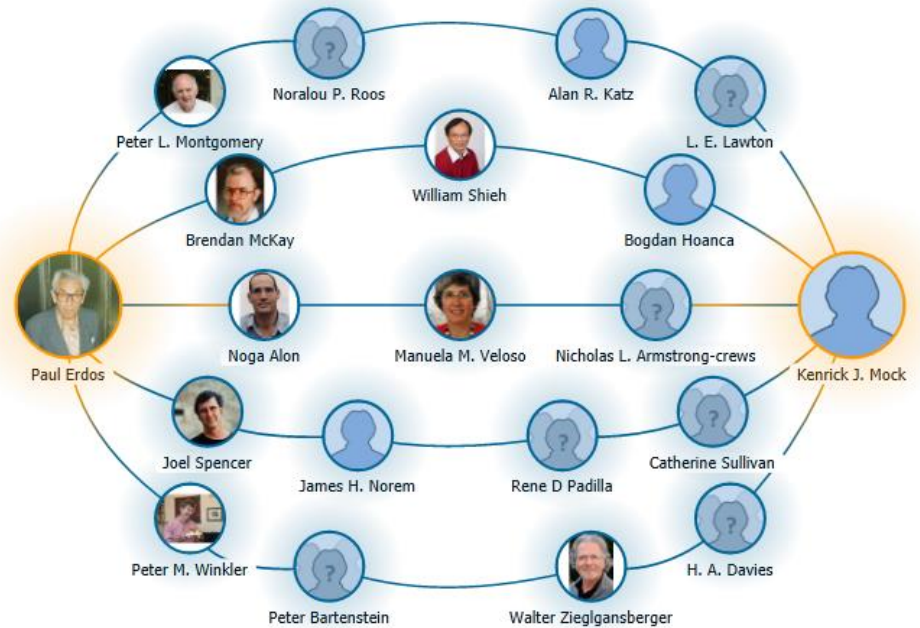
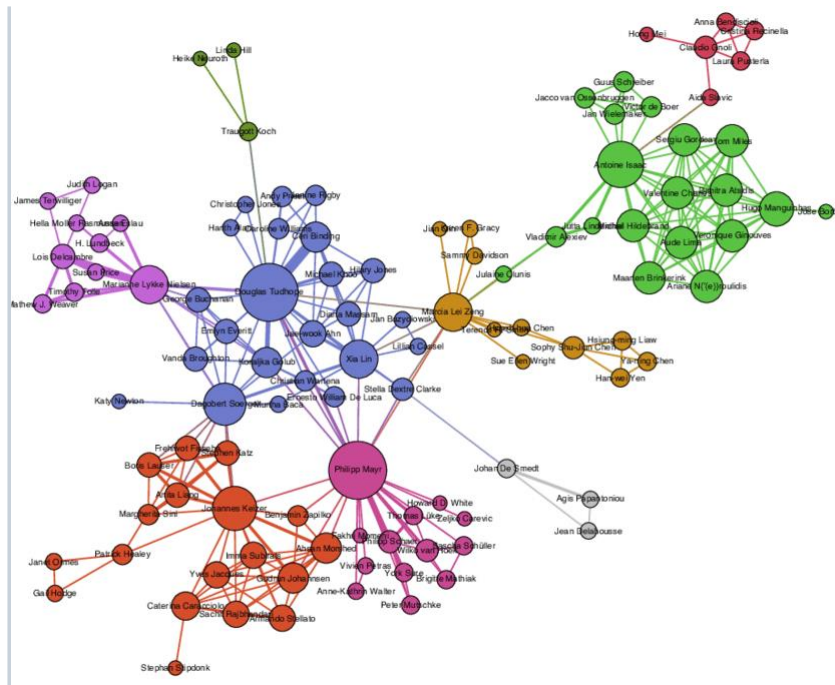
Who is the co-star hub of Iranian movies?!



This slide is borrowed from Dr. Aliakbari (SBU)



# Co-authorship Network

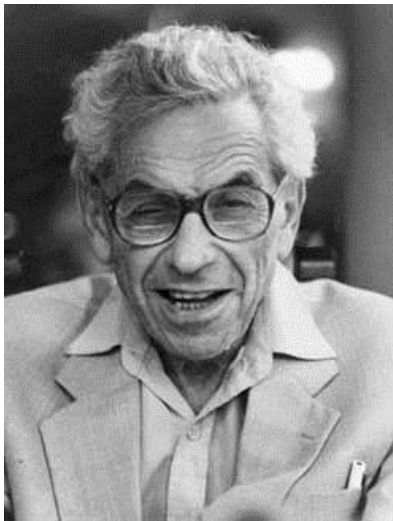


**Nodes: all publication authors**

**A link exists between two authors if they are coauthors in a publication**

# Co-authorship Network

- **Erdős number:** is the collaboration distance with mathematician **Paul Erdős**.



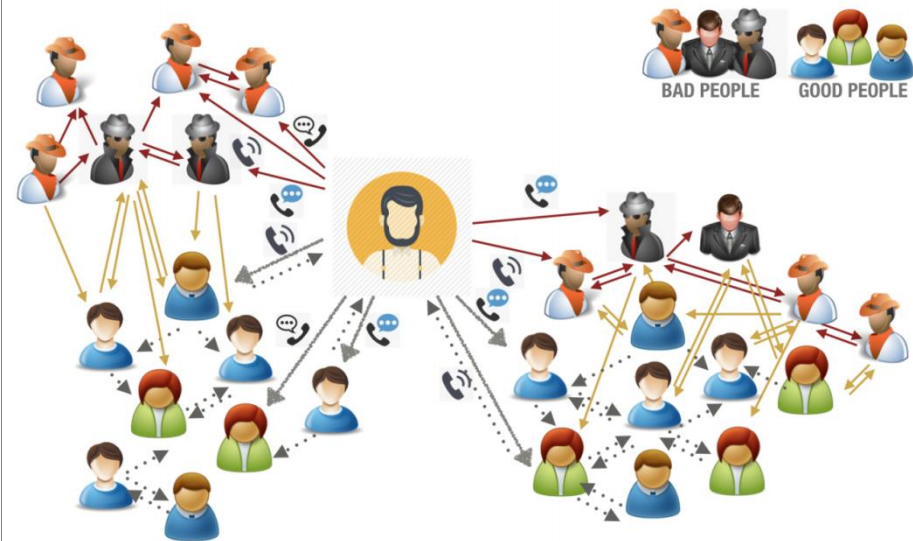
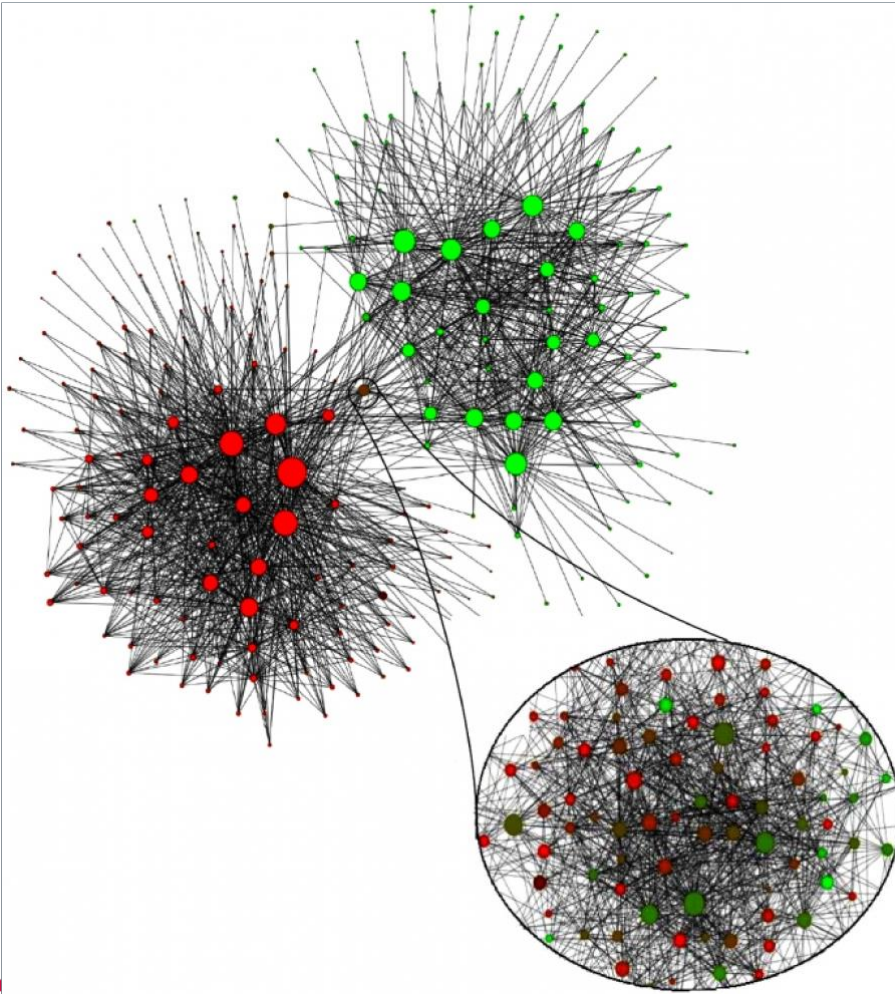
*Small world network*

## Distribution in Dec.2010

|                 |     |              |
|-----------------|-----|--------------|
| Erdős number 0  | --- | 1 person     |
| Erdős number 1  | --- | 504 people   |
| Erdős number 2  | --- | 6593 people  |
| Erdős number 3  | --- | 33605 people |
| Erdős number 4  | --- | 83642 people |
| Erdős number 5  | --- | 87760 people |
| Erdős number 6  | --- | 40014 people |
| Erdős number 7  | --- | 11591 people |
| Erdős number 8  | --- | 3146 people  |
| Erdős number 9  | --- | 819 people   |
| Erdős number 10 | --- | 244 people   |
| Erdős number 11 | --- | 68 people    |
| Erdős number 12 | --- | 23 people    |
| Erdős number 13 | --- | 5 people     |

\* Two persons are linked if they are coauthors of an article.

# Phone-call networks



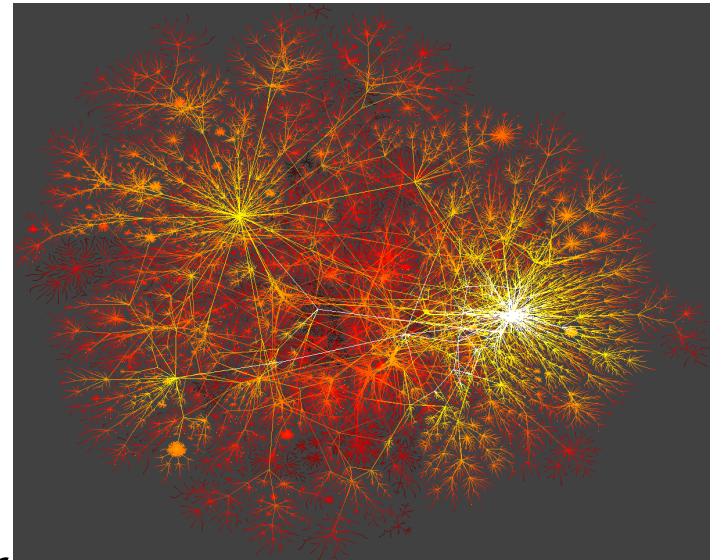
The background features a complex network diagram with numerous nodes (represented by small circles) and connecting lines (edges). The nodes are arranged in a non-uniform, interconnected pattern, suggesting a network structure. The lines are thin and dark, creating a web-like appearance. The overall color scheme is light blue and white, with a subtle gradient. The text 'Technological Networks' is prominently displayed in the center in a bold, blue, sans-serif font. The text is slightly shadowed, giving it a three-dimensional appearance as if it's floating above the network.

# Technological Networks

# Technological networks

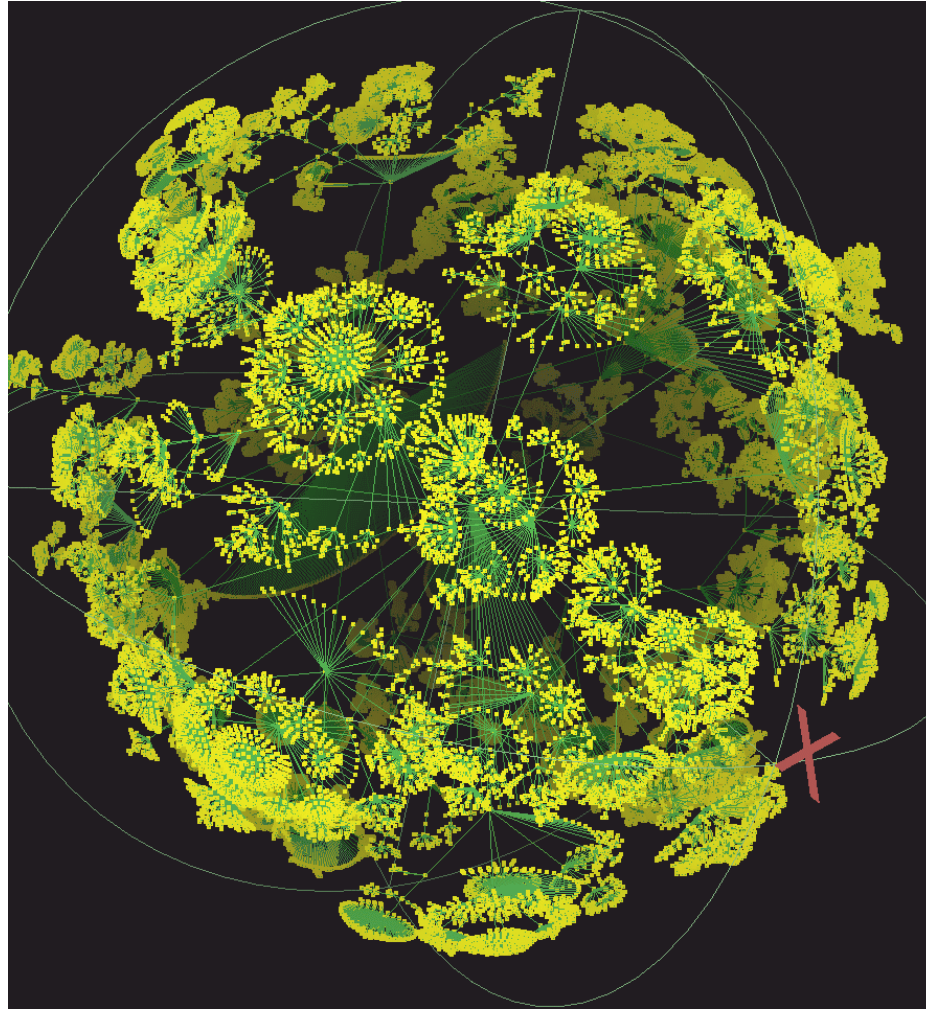
---

- Networks built for distribution of commodity
  - *The Internet*
    - *router level, AS level*
  - *Power Grids*
  - *Airline networks*
  - *Telephone networks*
  - *Transportation Networks*
    - *roads, railways, pedestrian traffic*



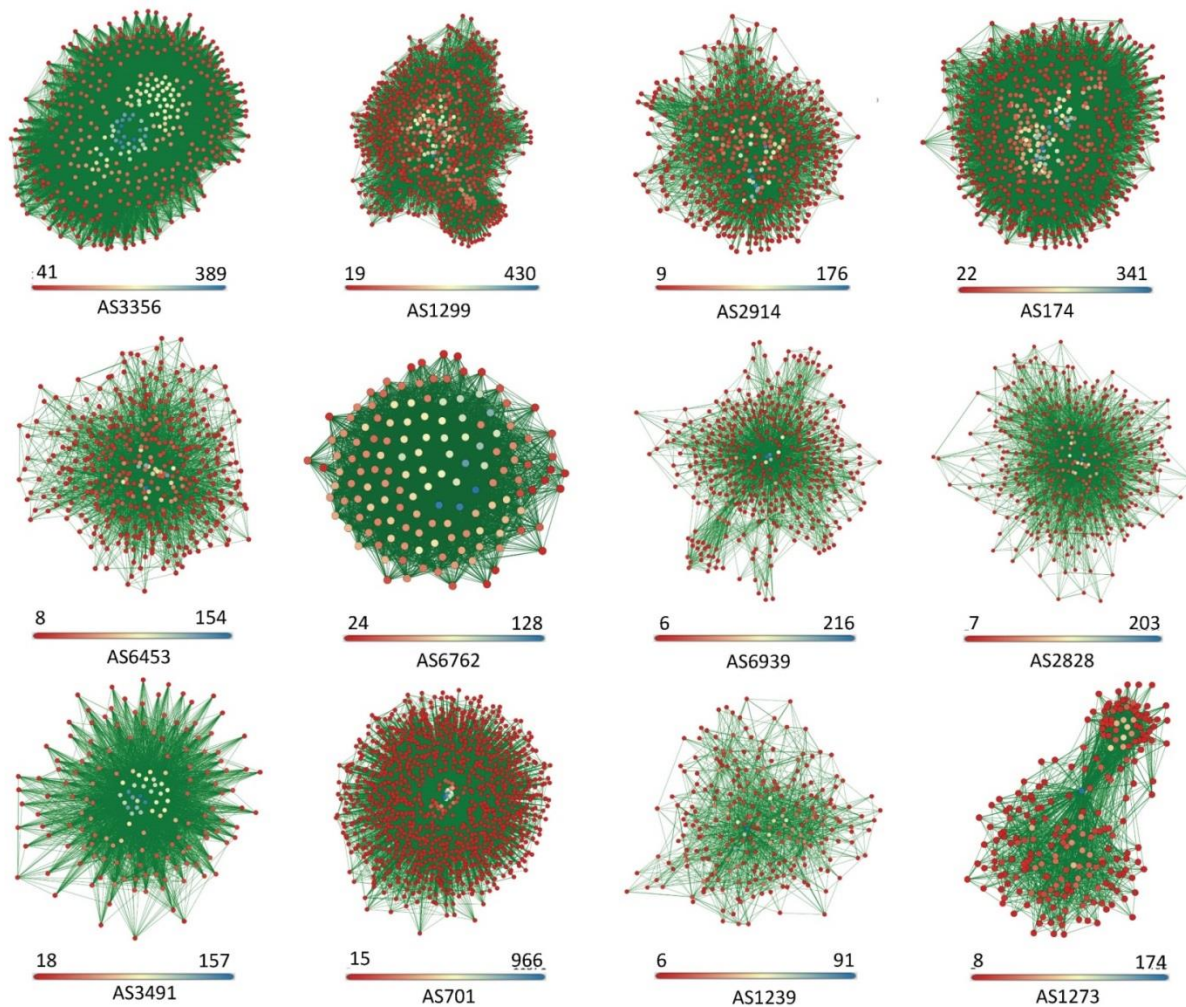
# Routers

---





# Internet Core Networks (AS level)

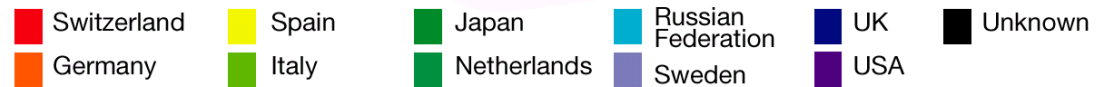
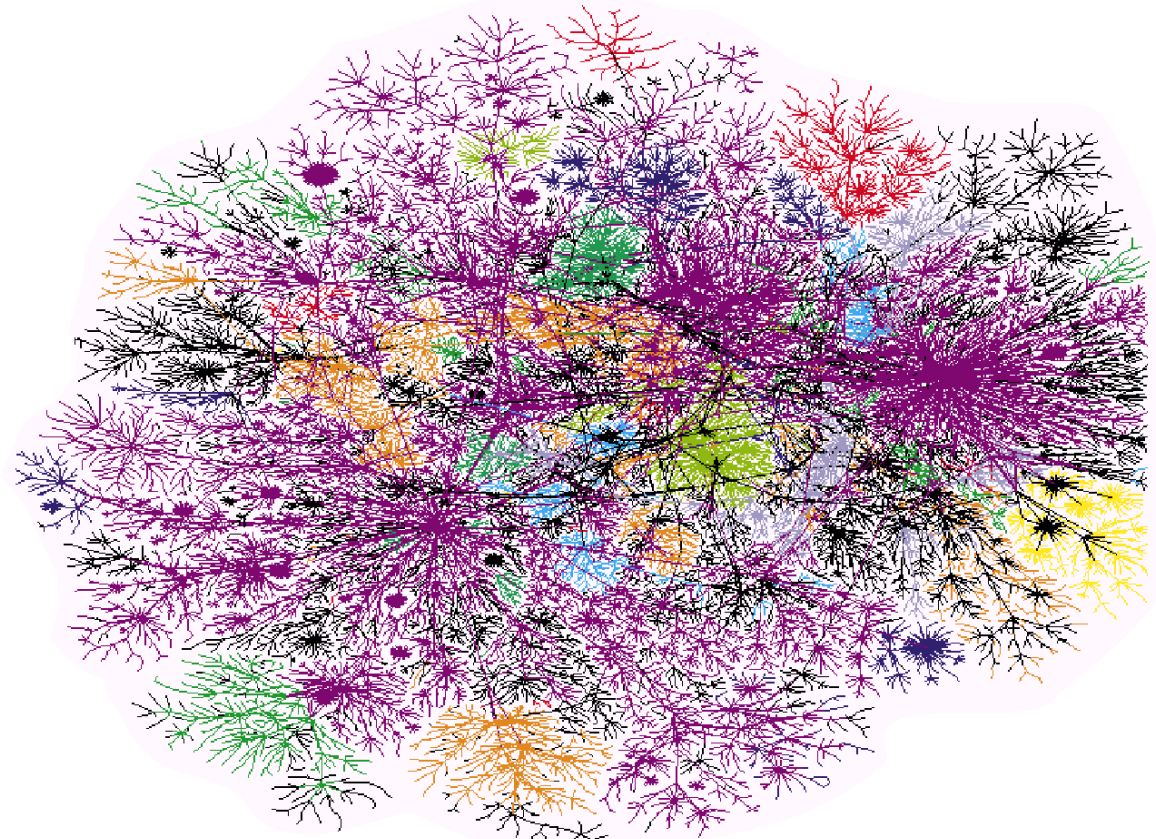


# Internet Map

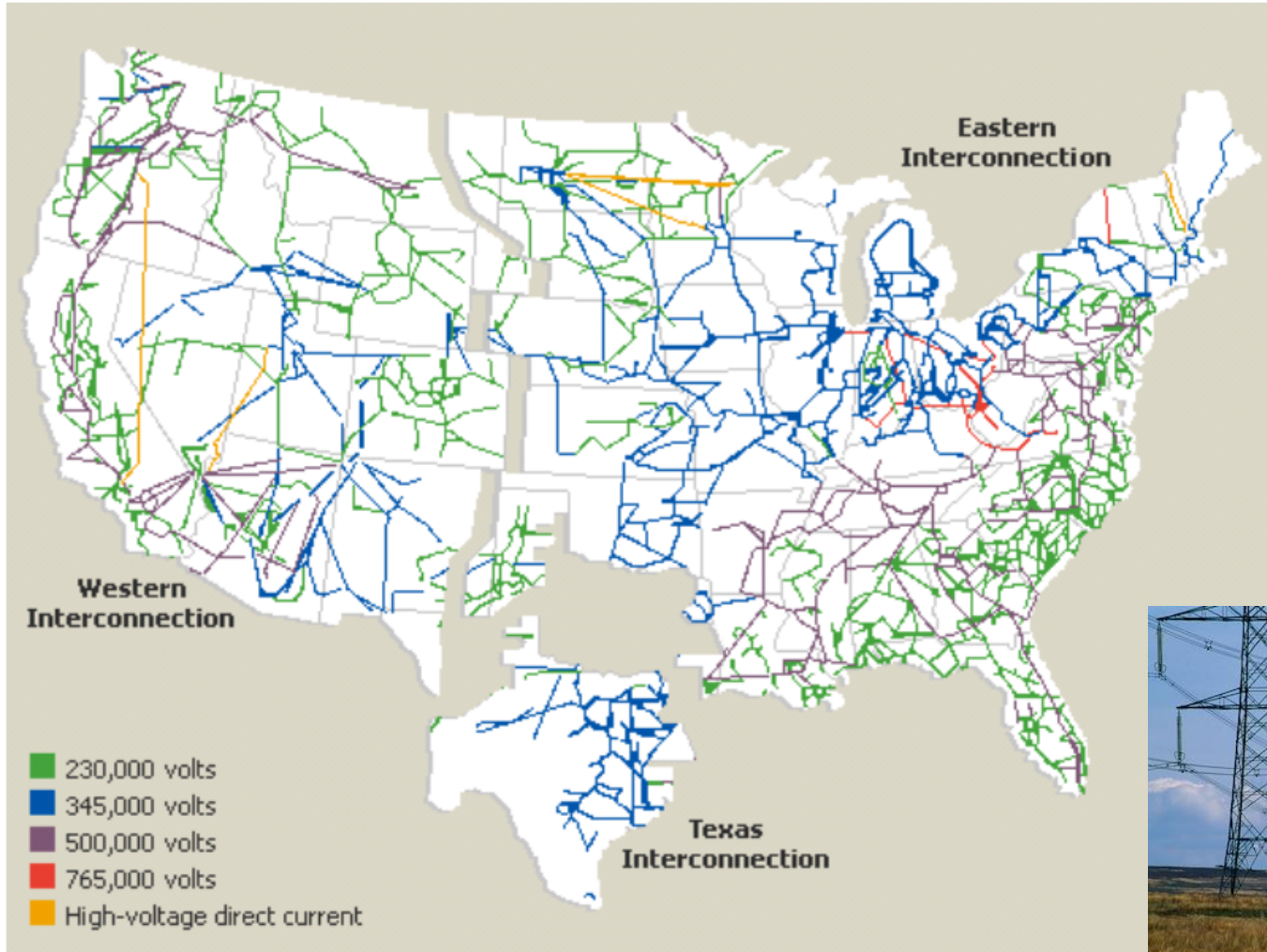
Internet as measured by Hal Burch and Bill Cheswick's [Internet Mapping Project](#).



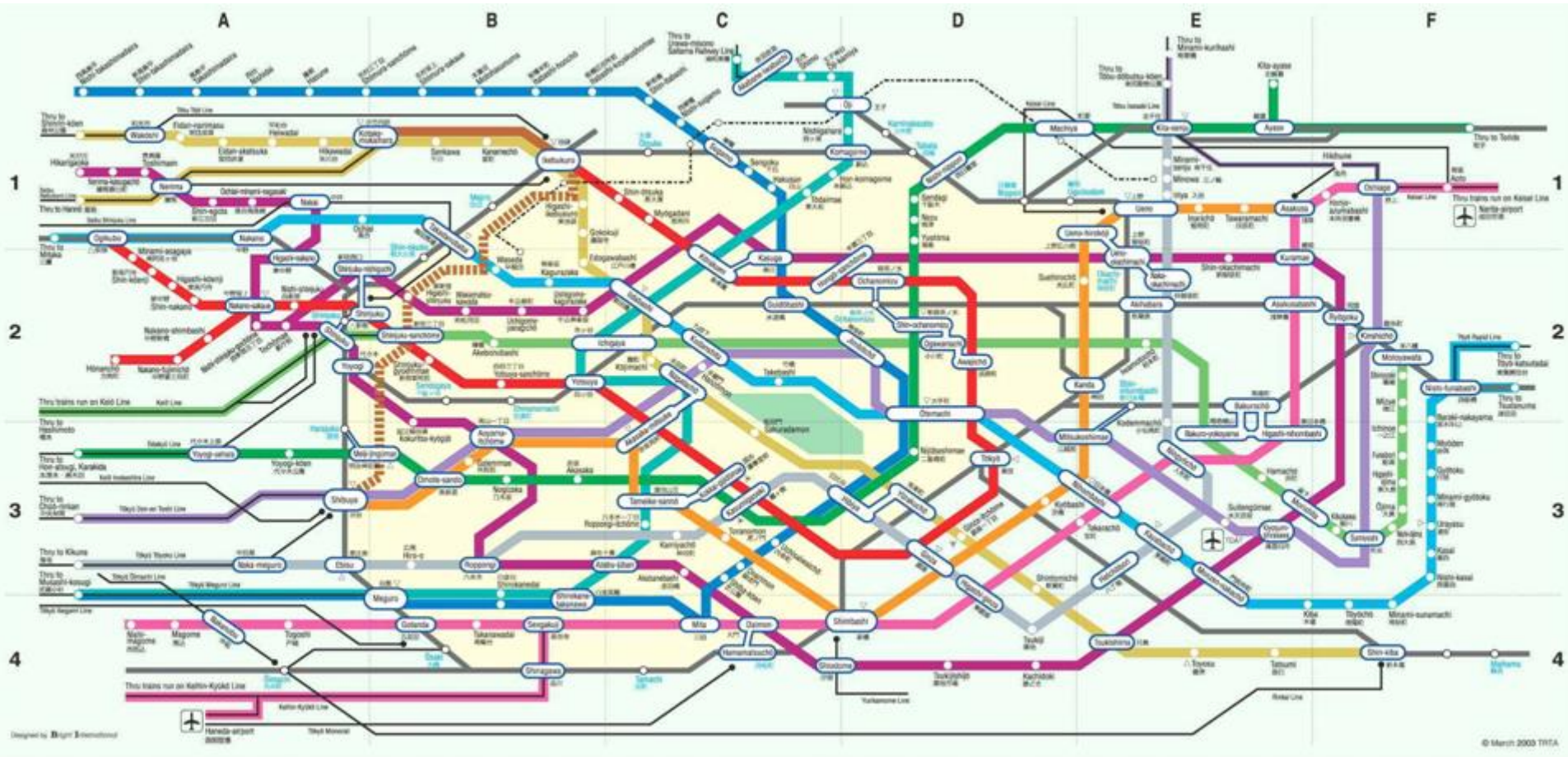
**Note:** Internet != Web



# Power networks

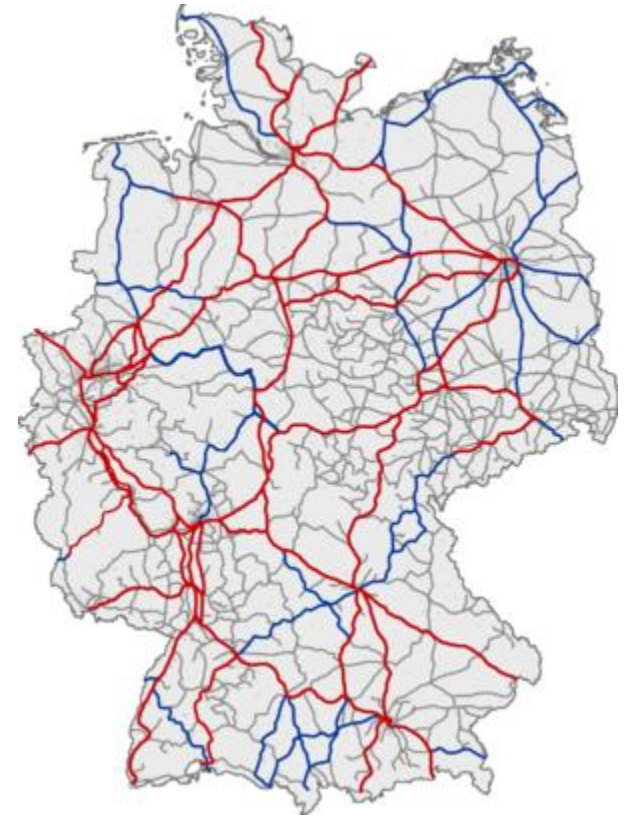
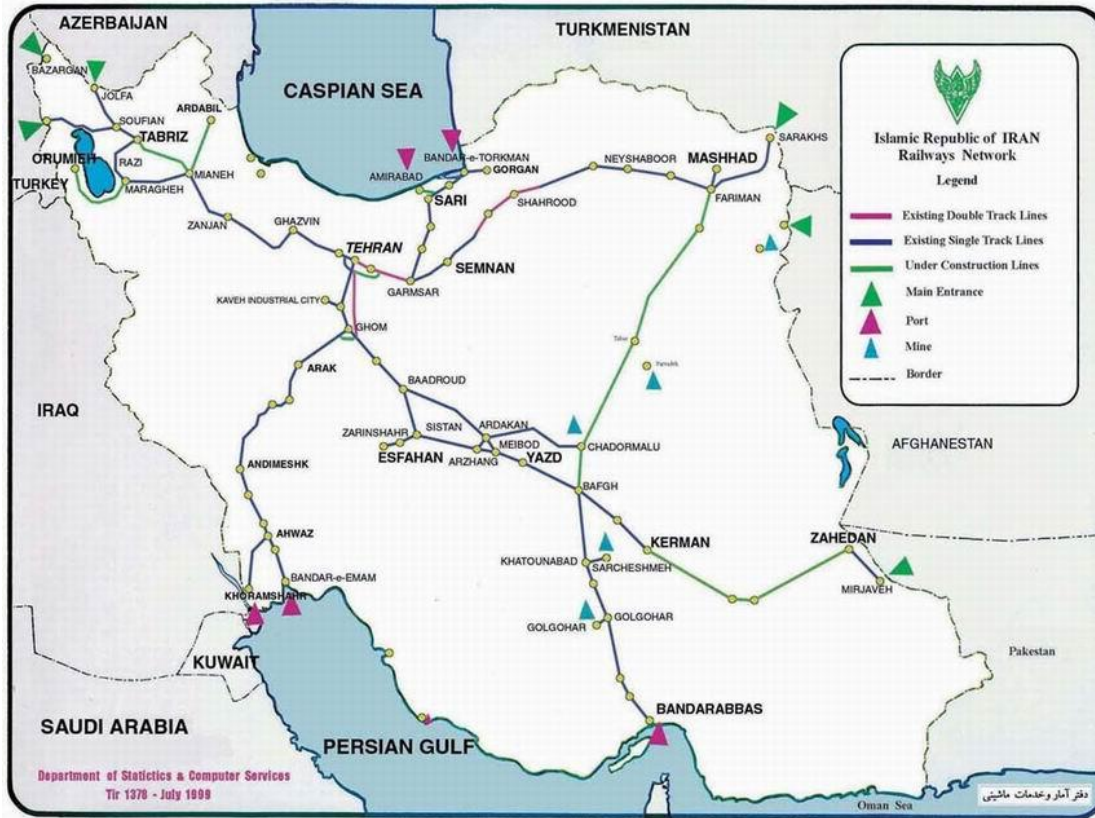


# Subway maps

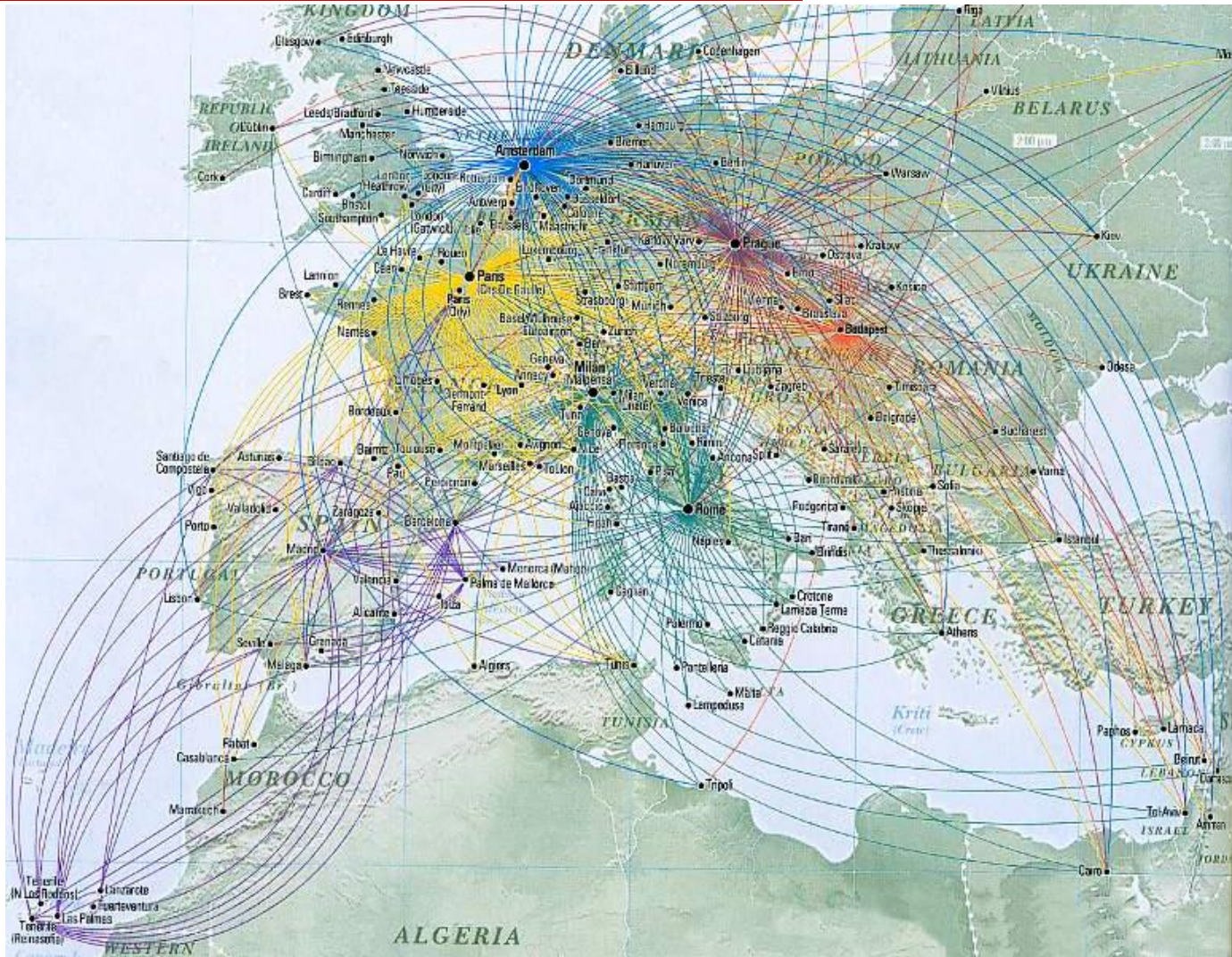


Source: TRTA, March 2003 - Tokyo rail map

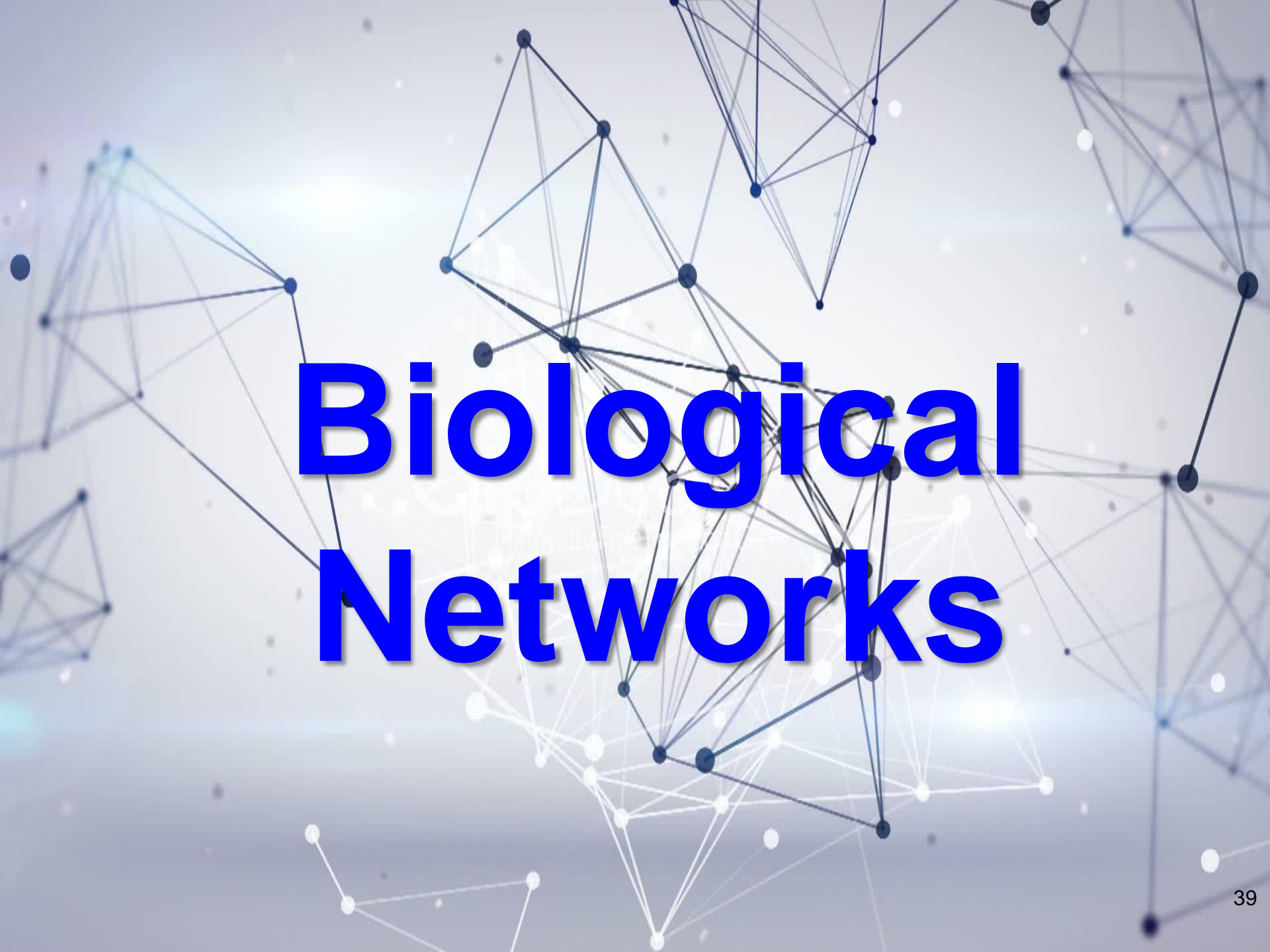
# Railway Maps



# Airline network



Source: Northwest Airlines WorldTraveler Magazine

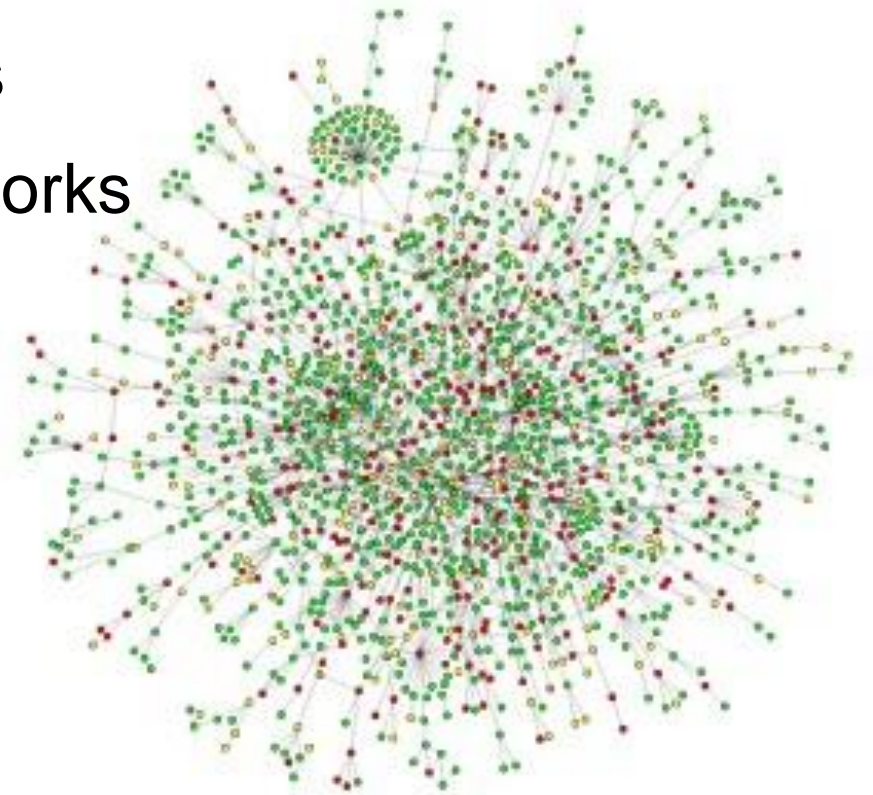
The background features a complex network diagram with numerous nodes and connecting lines, rendered in shades of blue and white against a light blue gradient. The nodes are represented by small circles, and the lines are thin, creating a web-like structure that fills the entire frame.

# Biological Networks

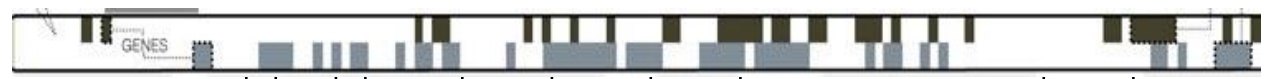
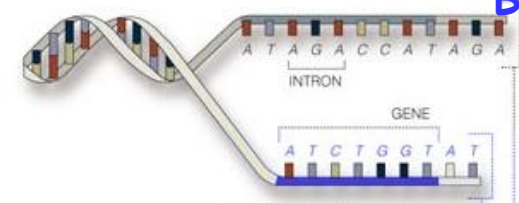
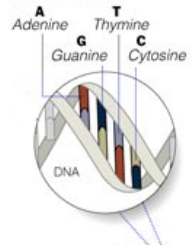
# Biological networks

---

- Biological systems represented as networks
  - Protein-Protein Interaction Networks
  - Gene regulation networks
  - Gene co-expression networks
  - Metabolic pathways
  - The Food Web
  - Neural Networks

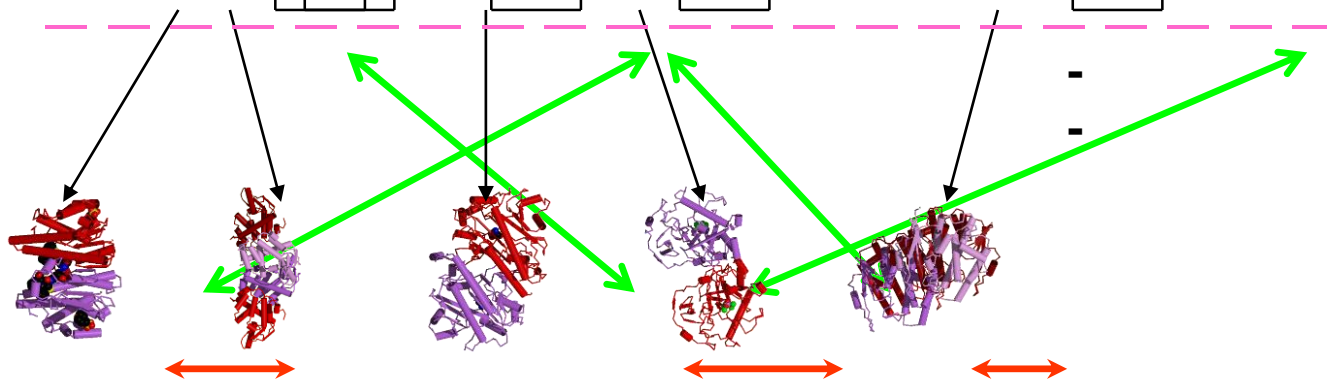






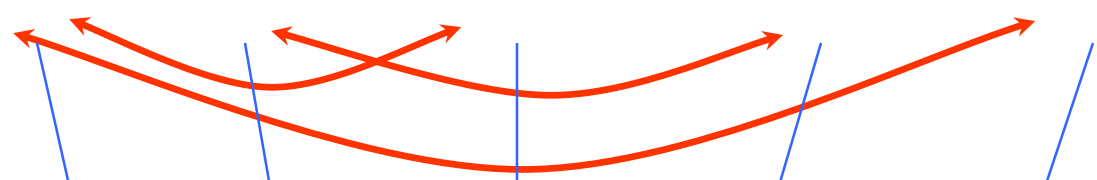
# GENOME

protein-gene interactions



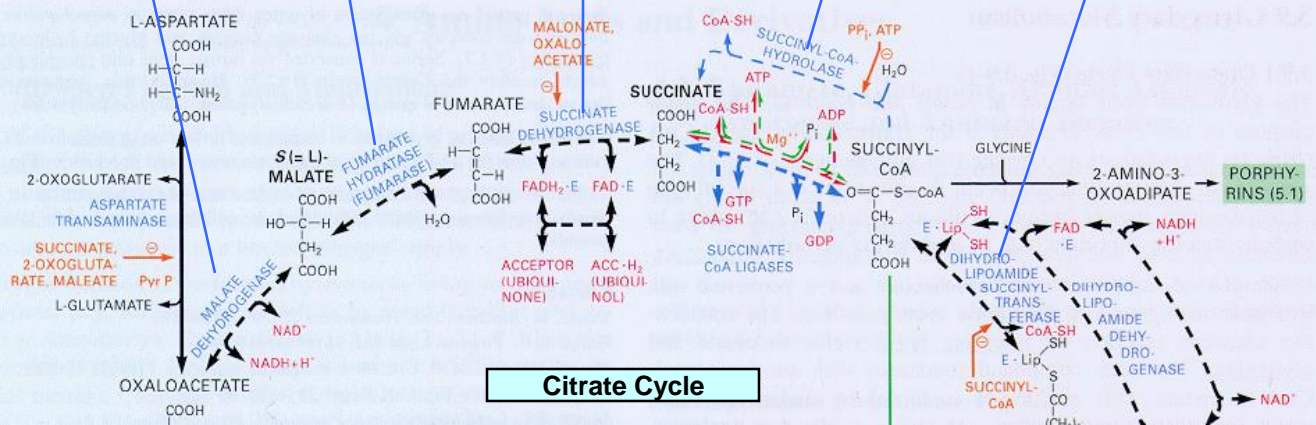
# PROTEOME

protein-protein interactions



# METABOLISM

Bio-chemical reactions



# Protein-Protein Interactions

Classifying the function of proteins in the interactome!

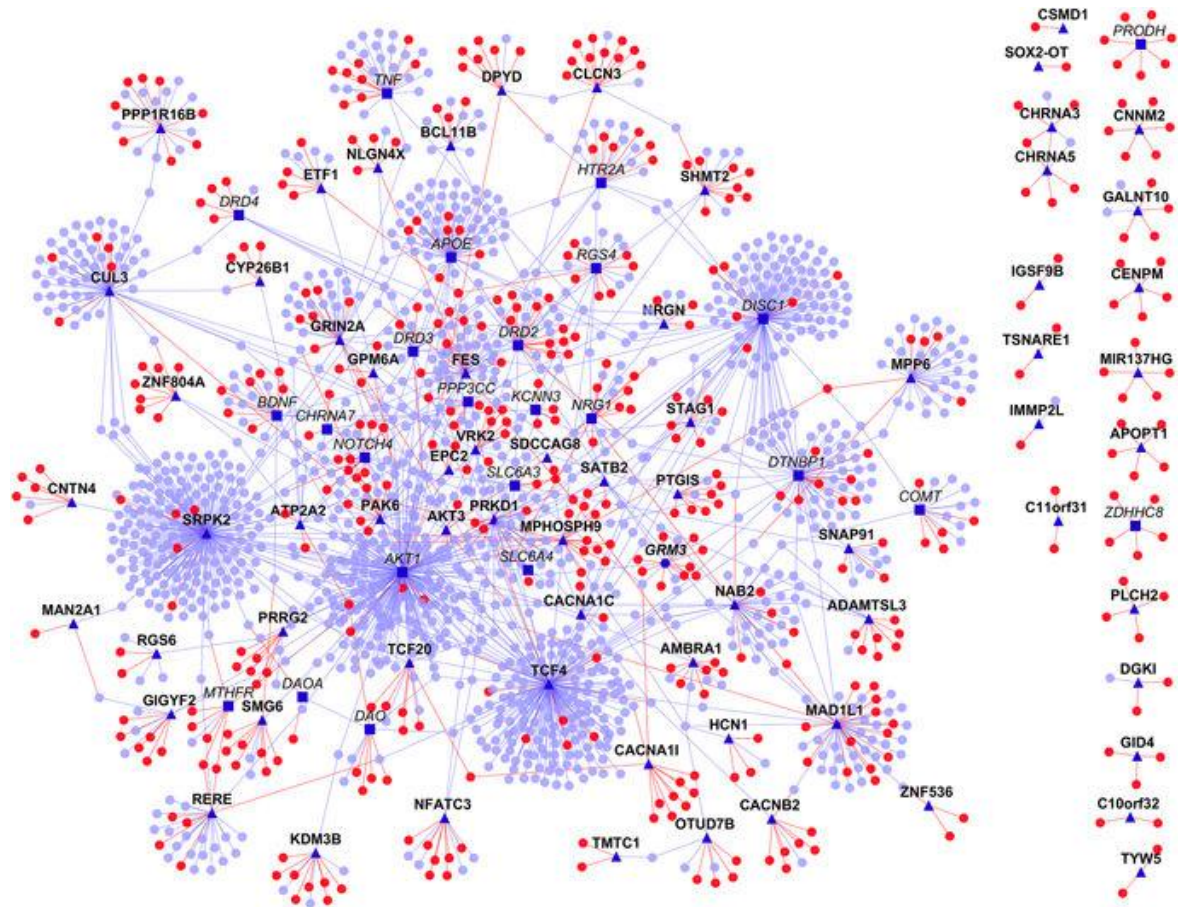
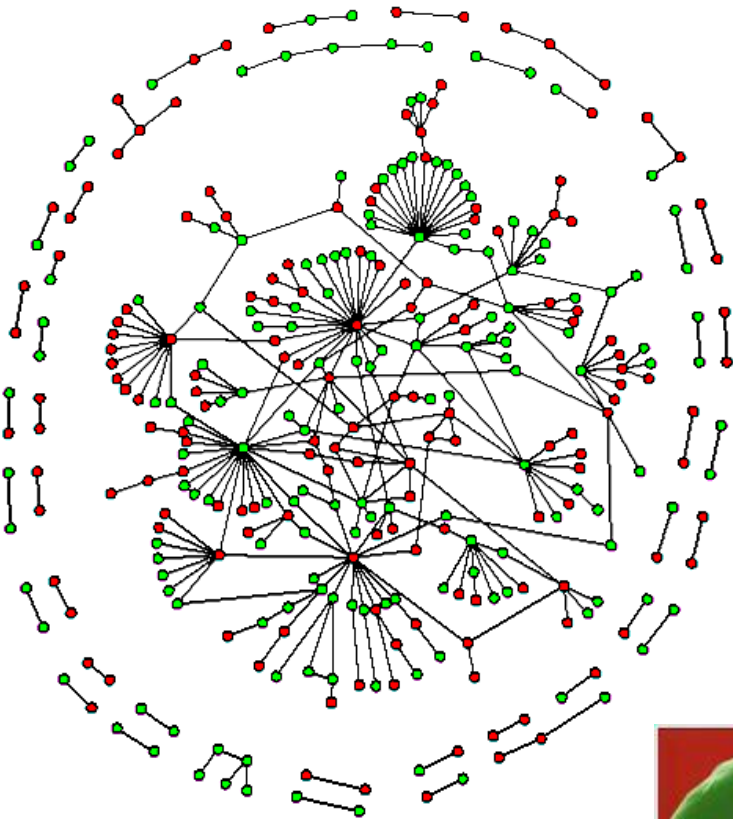
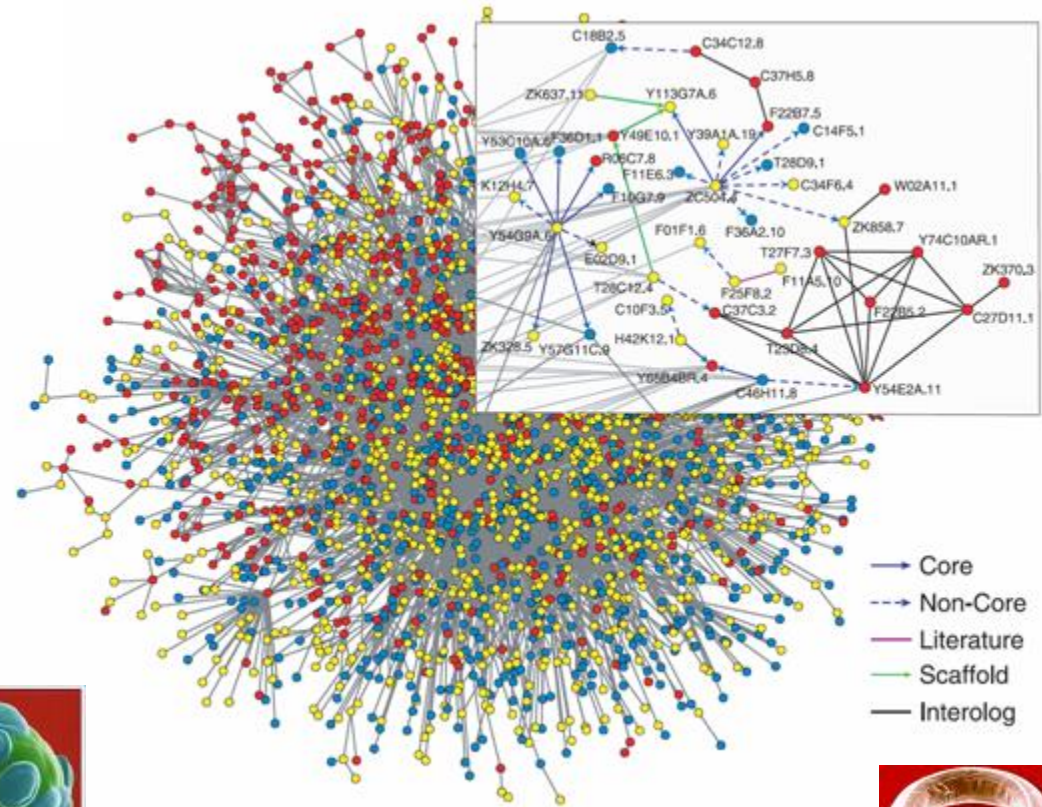


Image from: Ganapathiraju et al. 2016. [Schizophrenia interactome with 504 novel protein–protein interactions.](#) *Nature*.

# Protein binding networks



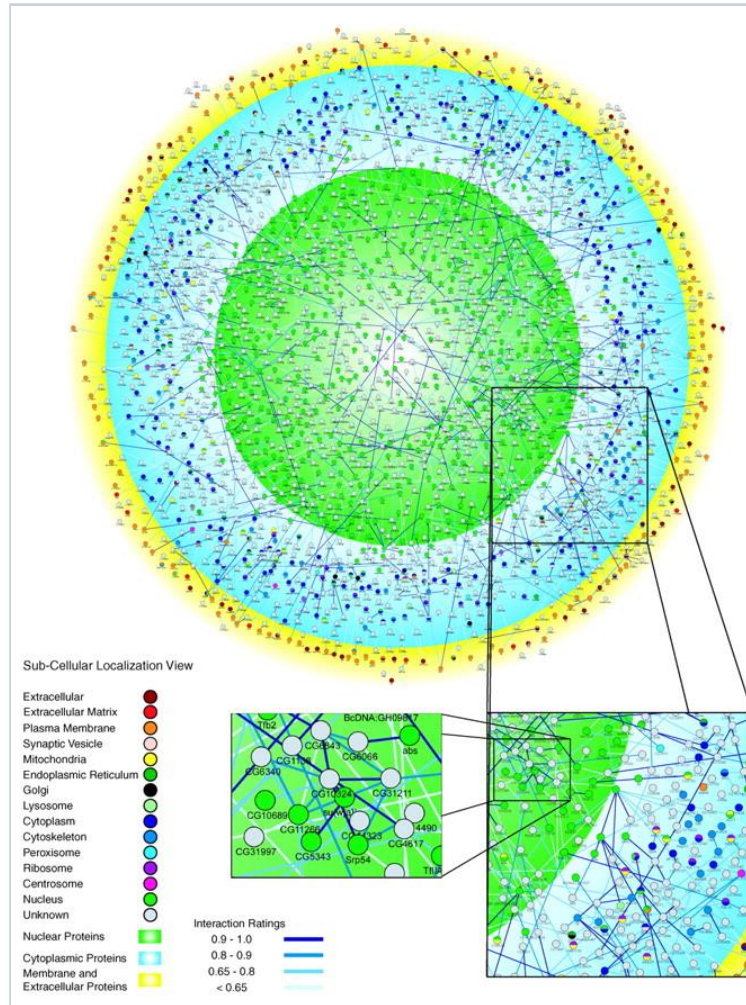
Baker's yeast *S. cerevisiae*  
(only nuclear proteins shown)



Nematode worm *C. elegans*

# The Protein Network of Drosophila

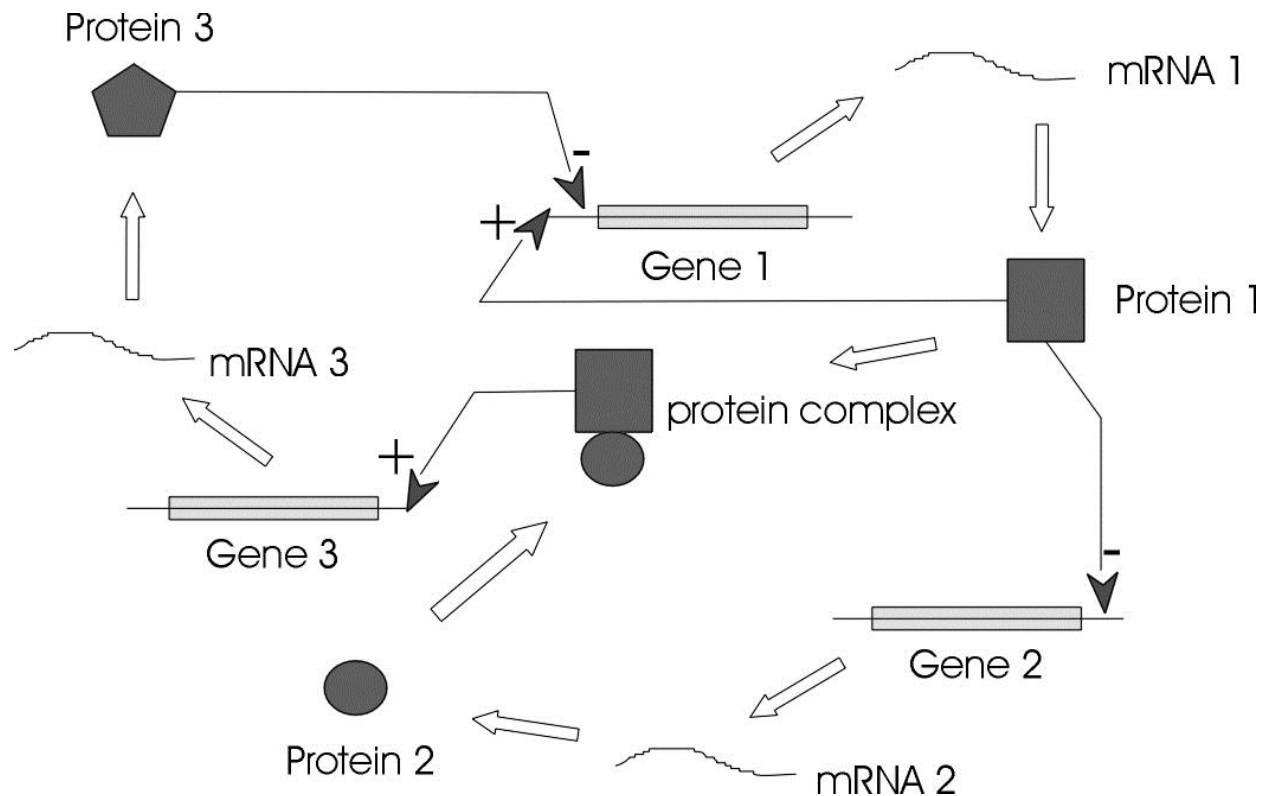
CuraGen Corporation  
Science, 2003





# Gene regulatory networks

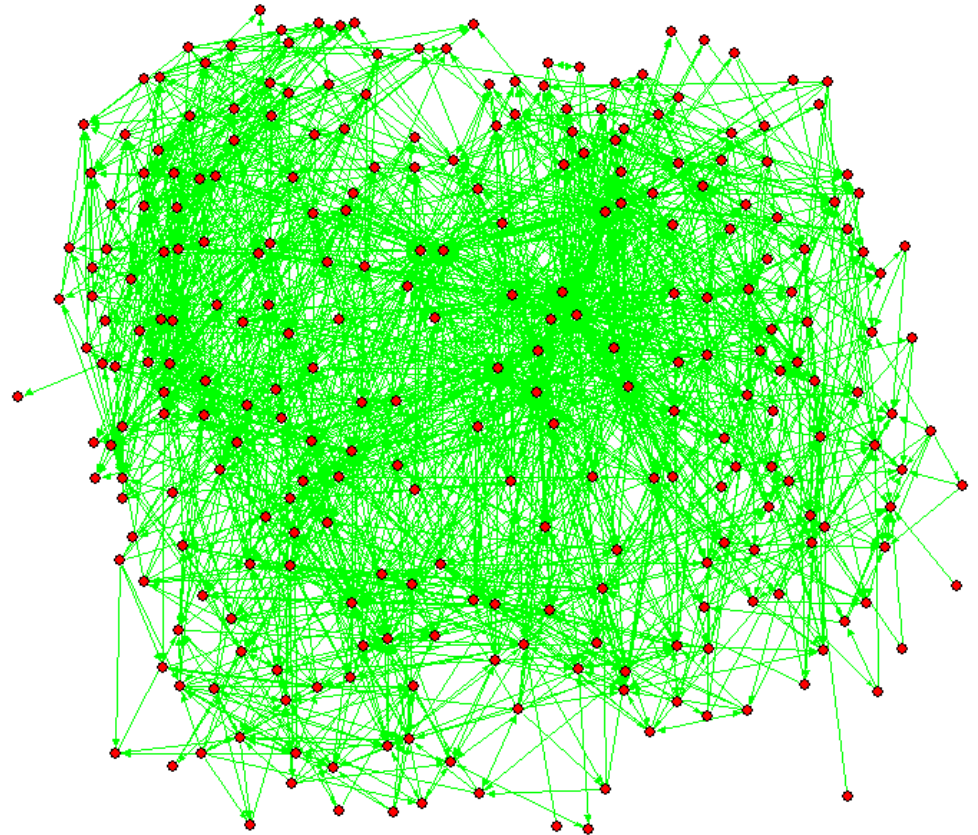
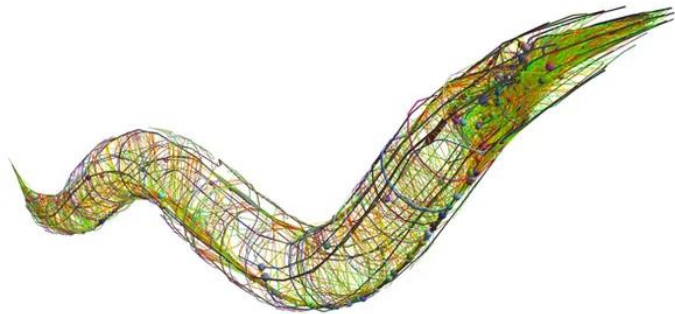
- Humans have 30,000 genes
- The complexity is in the interaction of genes
- Can we predict what result of the inhibition of one gene will be?



Source: <http://www.zaik.uni-koeln.de/bioinformatik/regulatorynets.html.en>

# C. Elegans neurons network

---



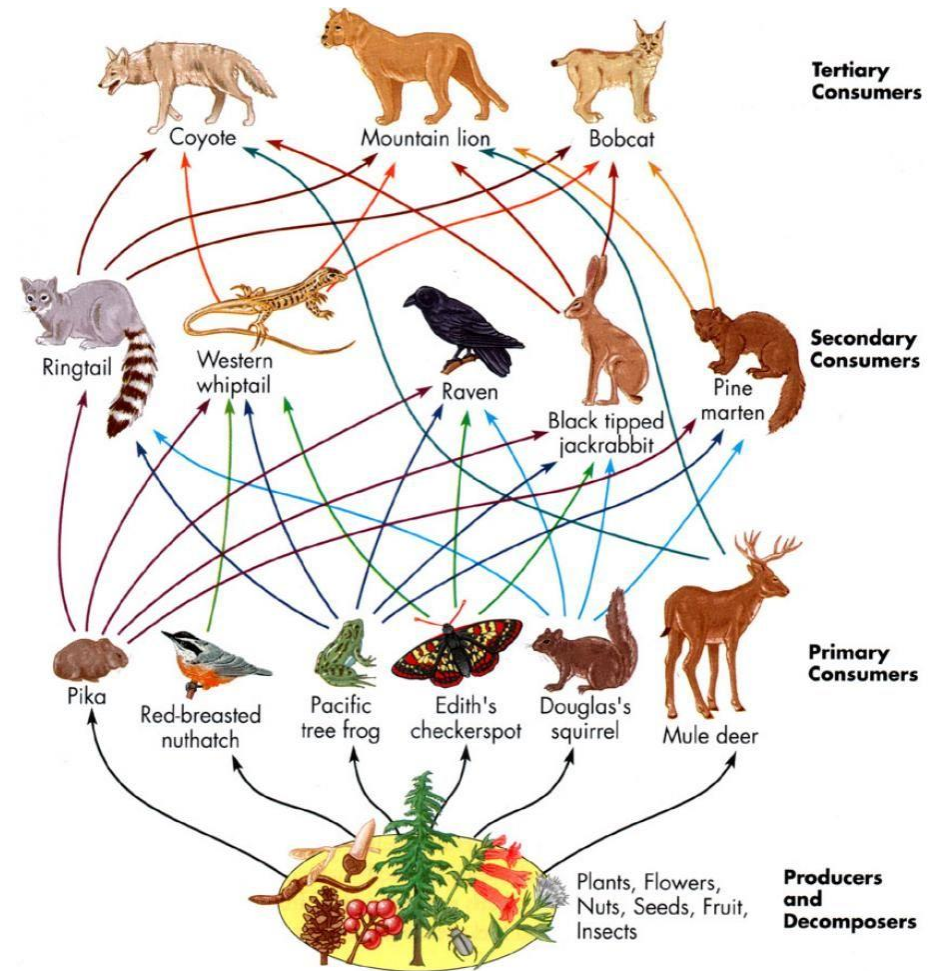
The map of all 302 neurons in the C. elegans nervous system

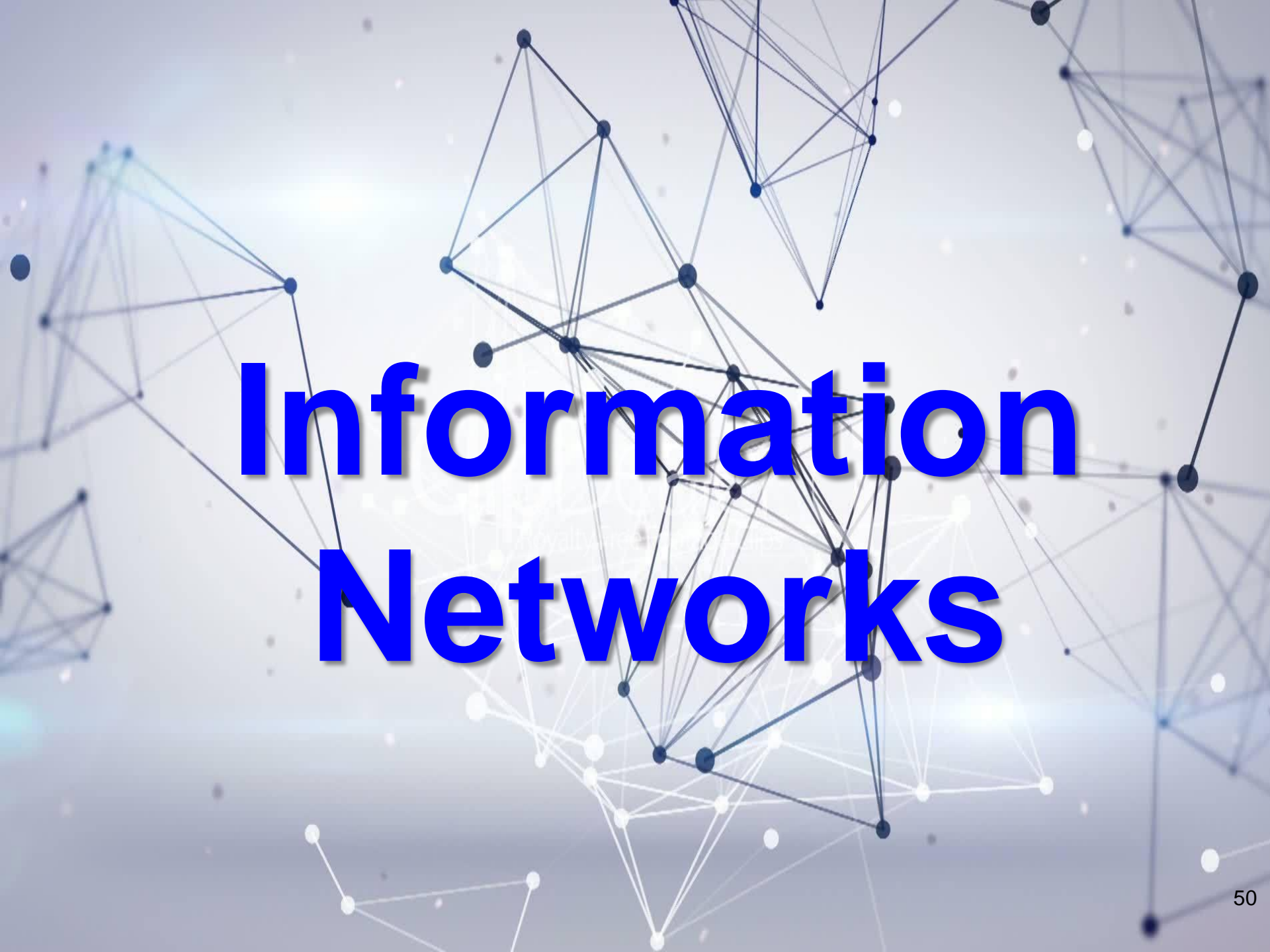




# Food Chain Network

Food web is an important conceptual tool for illustrating the feeding relationships among species within a community, revealing species interactions and community structure, and understanding the dynamics of energy transfer in an ecosystem



The background features a complex network of interconnected nodes and lines, rendered in shades of blue and white against a light blue gradient. The nodes are represented by small circles, and the connections are thin lines forming a web-like structure. The overall aesthetic is clean and modern, typical of a technology or data-related presentation.

# Information Networks

# Knowledge (Information) Networks

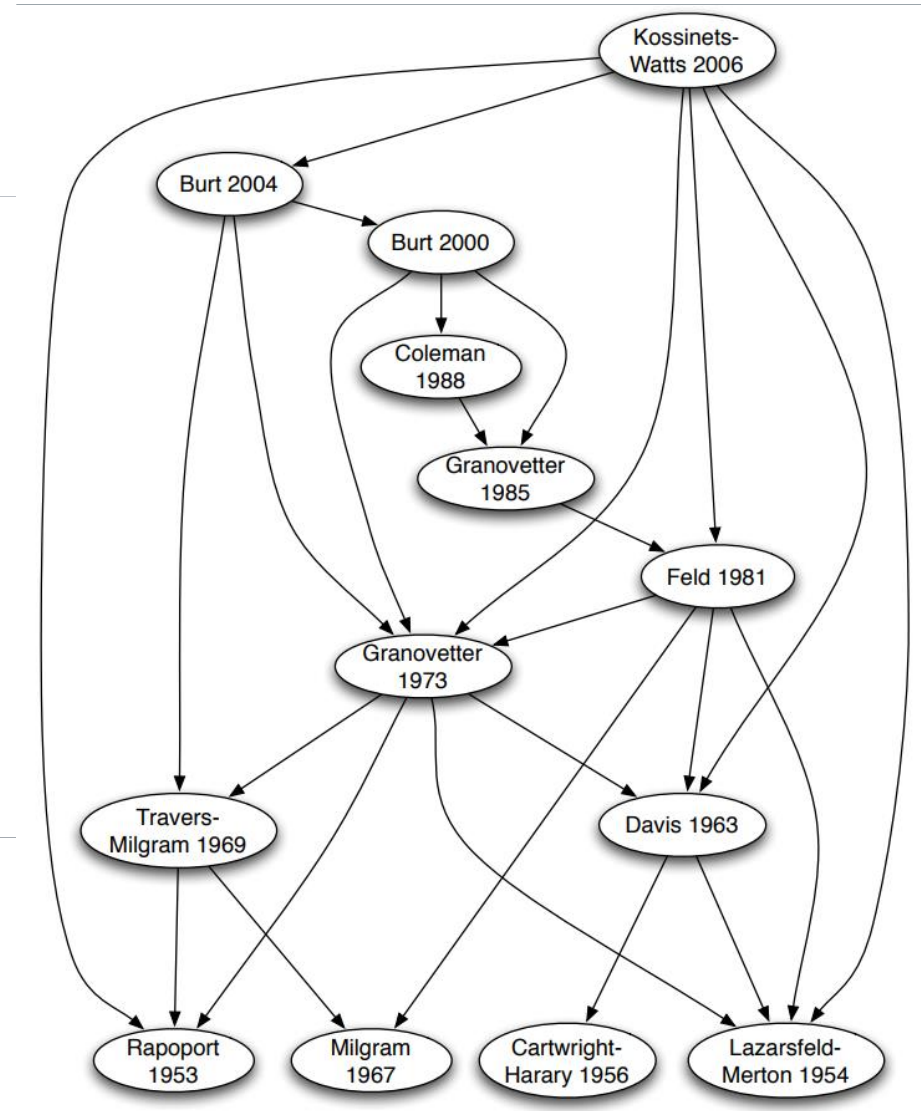
---

Nodes store information, links associate information

- Citation network (directed acyclic)
- The Web (directed)
- Peer-to-Peer networks
- Word networks
- Networks of Trust
- Software graphs

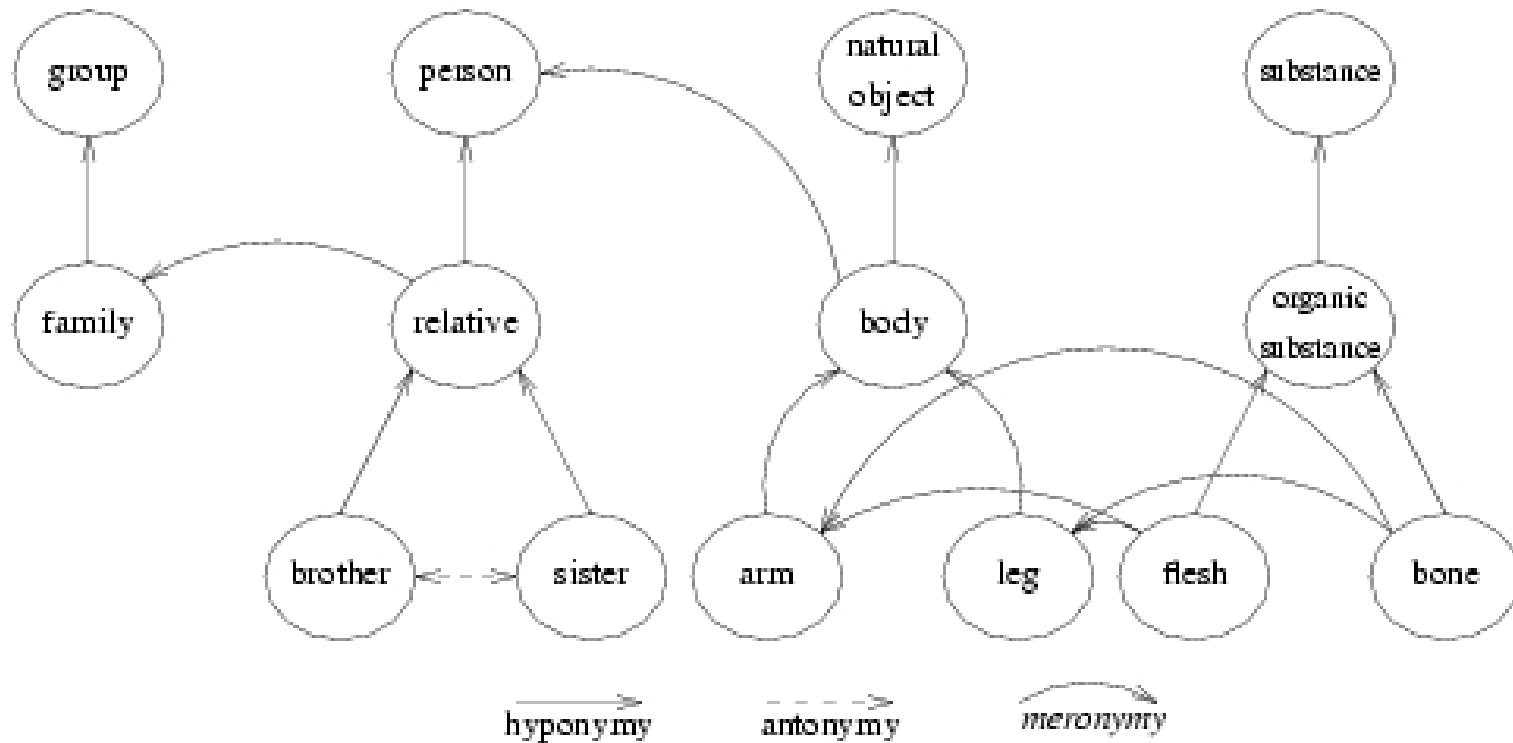


# Citation Network



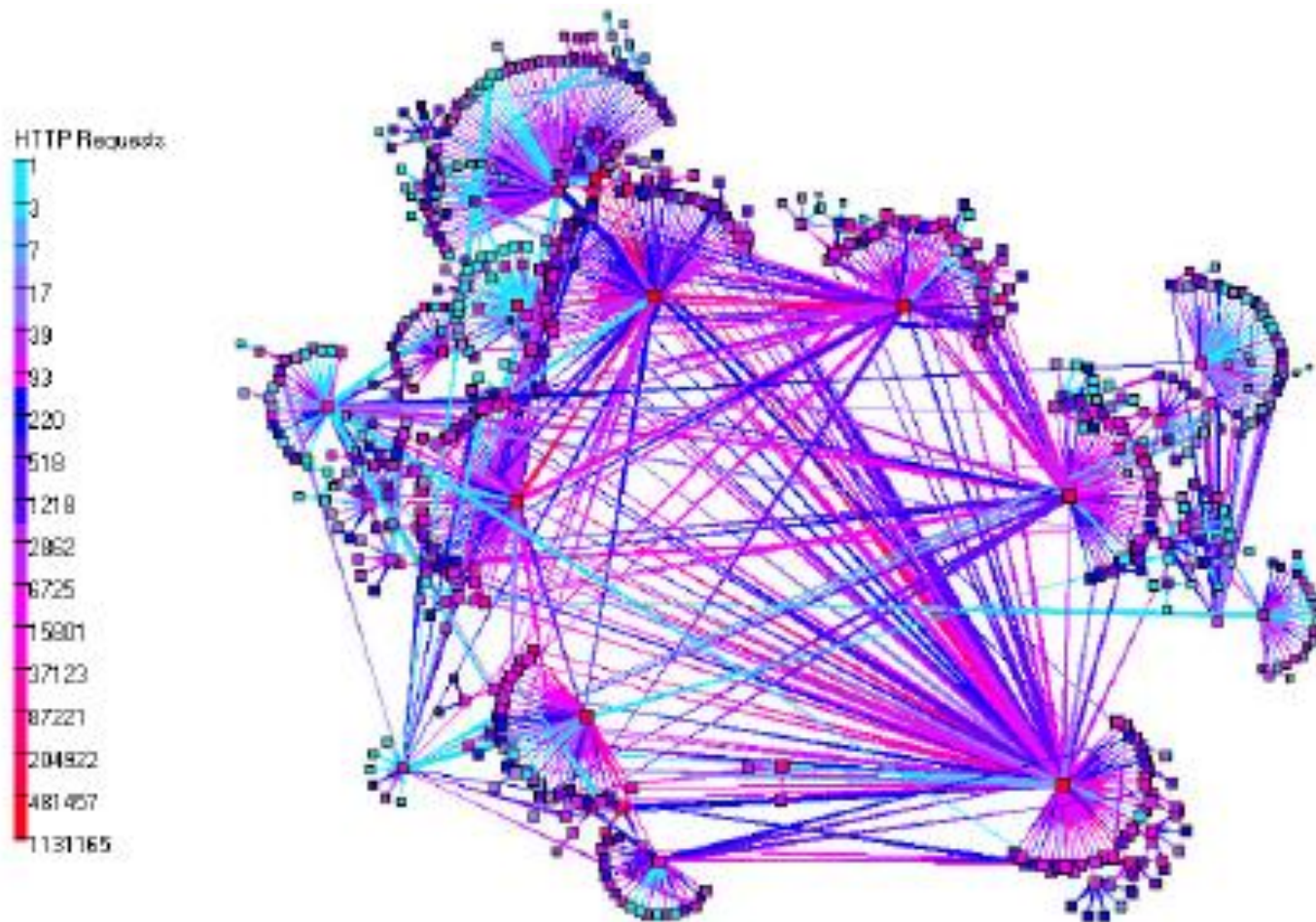
# Natural language processing

## Wordnet



Source: <http://wordnet.princeton.edu>

# World Wide Web

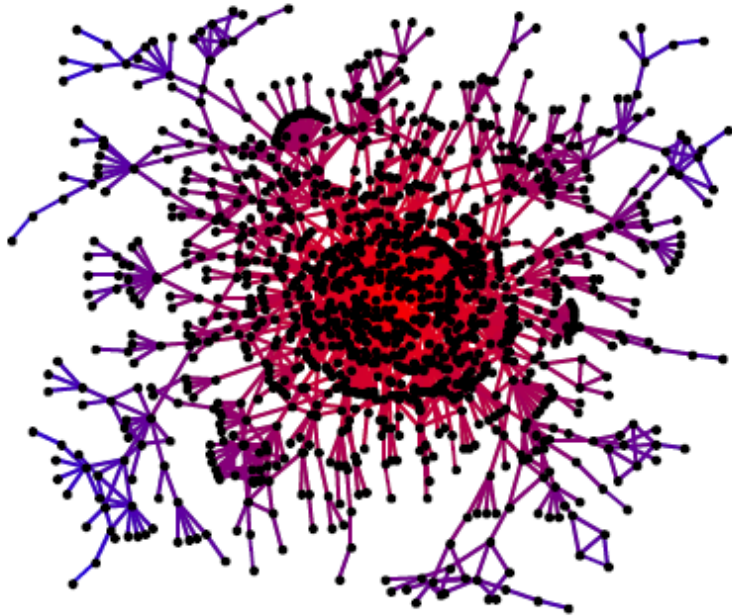


*Hierarchical topology of the international Web cache*

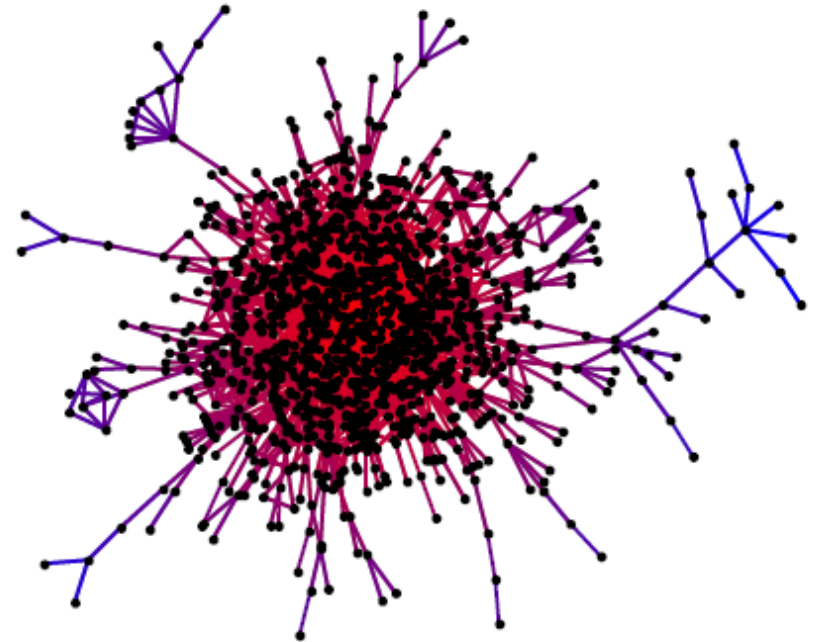
(Bradley Huffaker, <http://www.caida.org/tools/visualization/plankton>)

# Networks of personal homepages

---



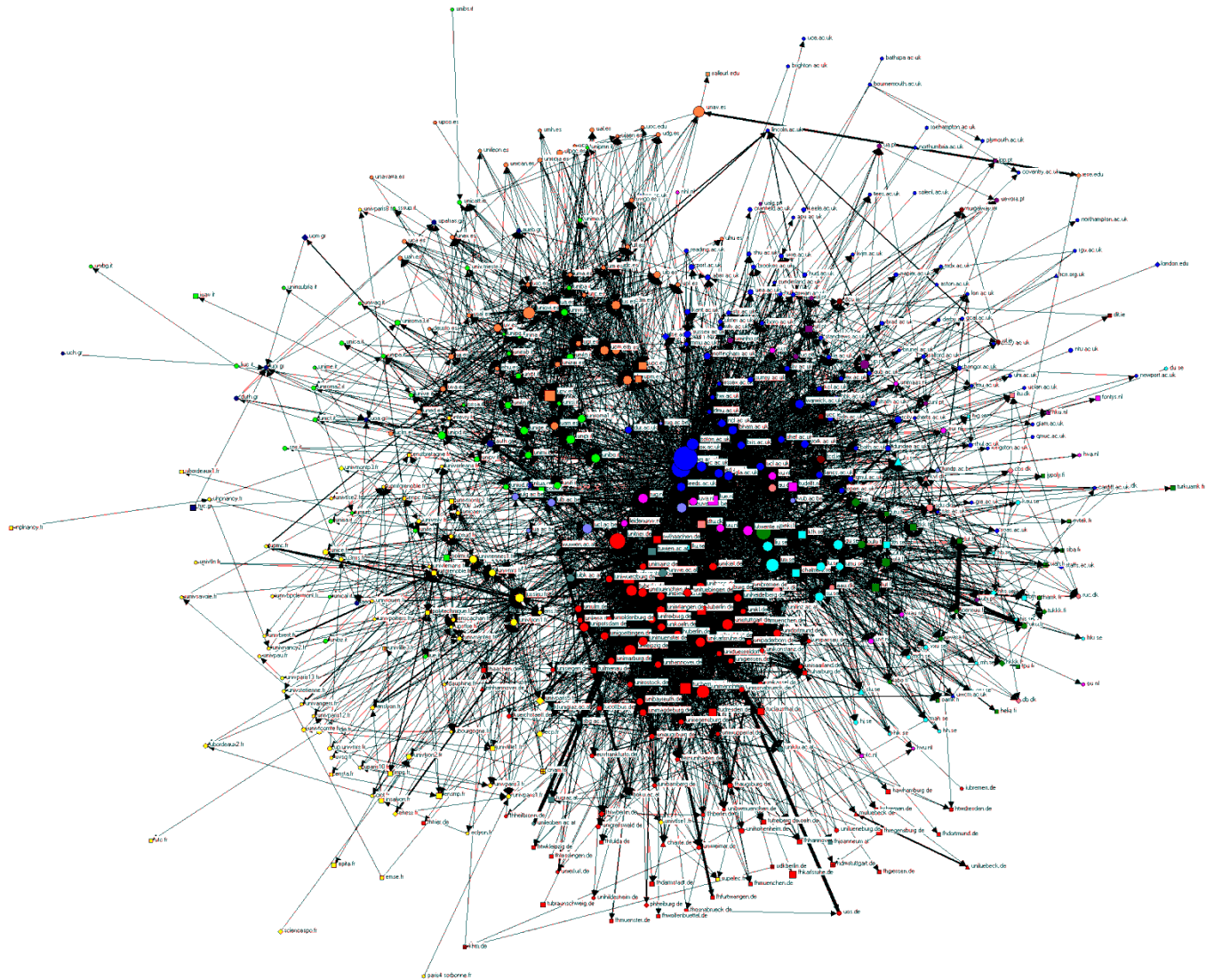
Stanford



MIT

Source: Lada A. Adamic and Eytan Adar, 'Friends and neighbors on the web', *Social Networks*, 25(3):211-230, July 2003

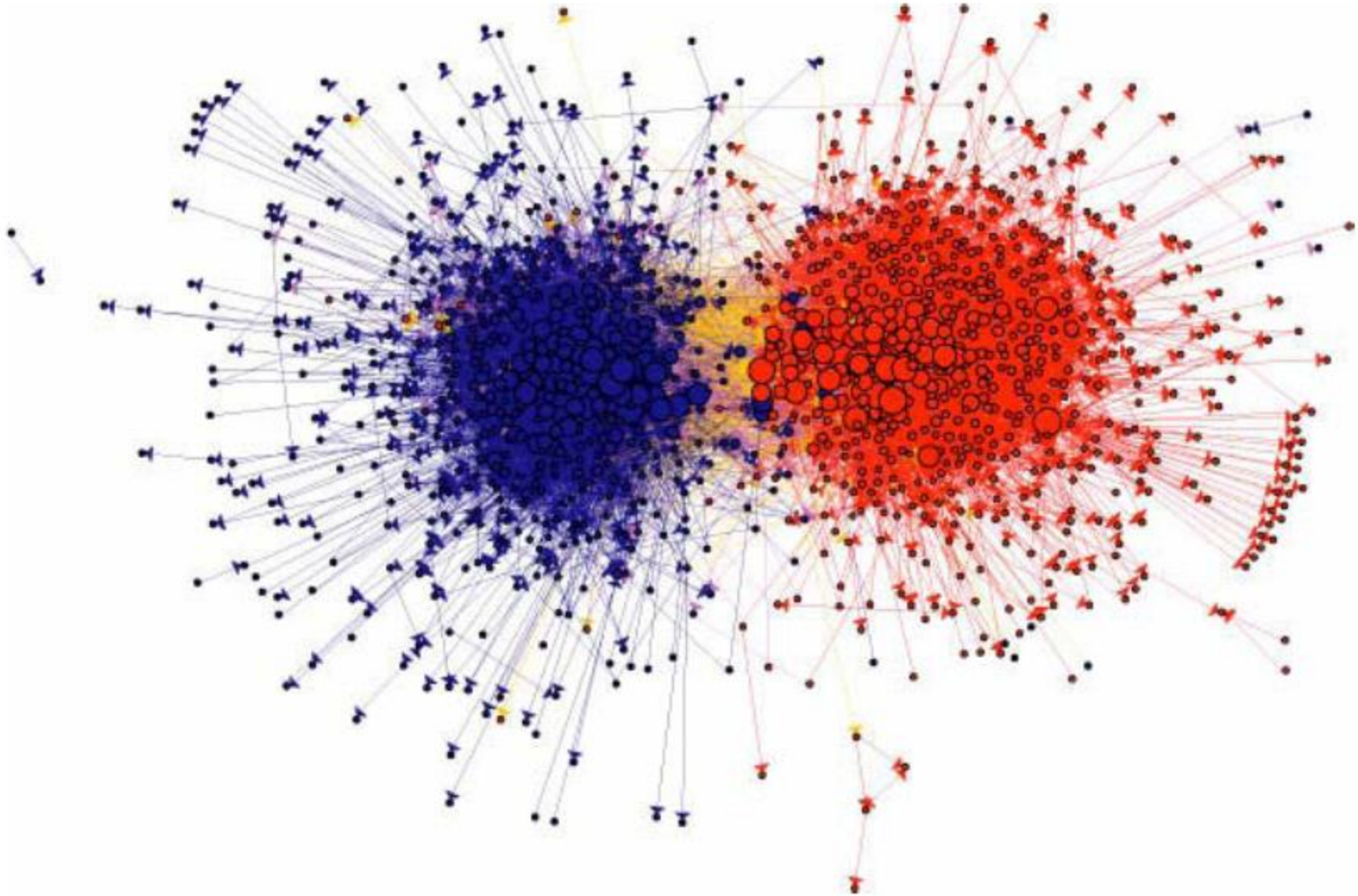
# European University Web Pages



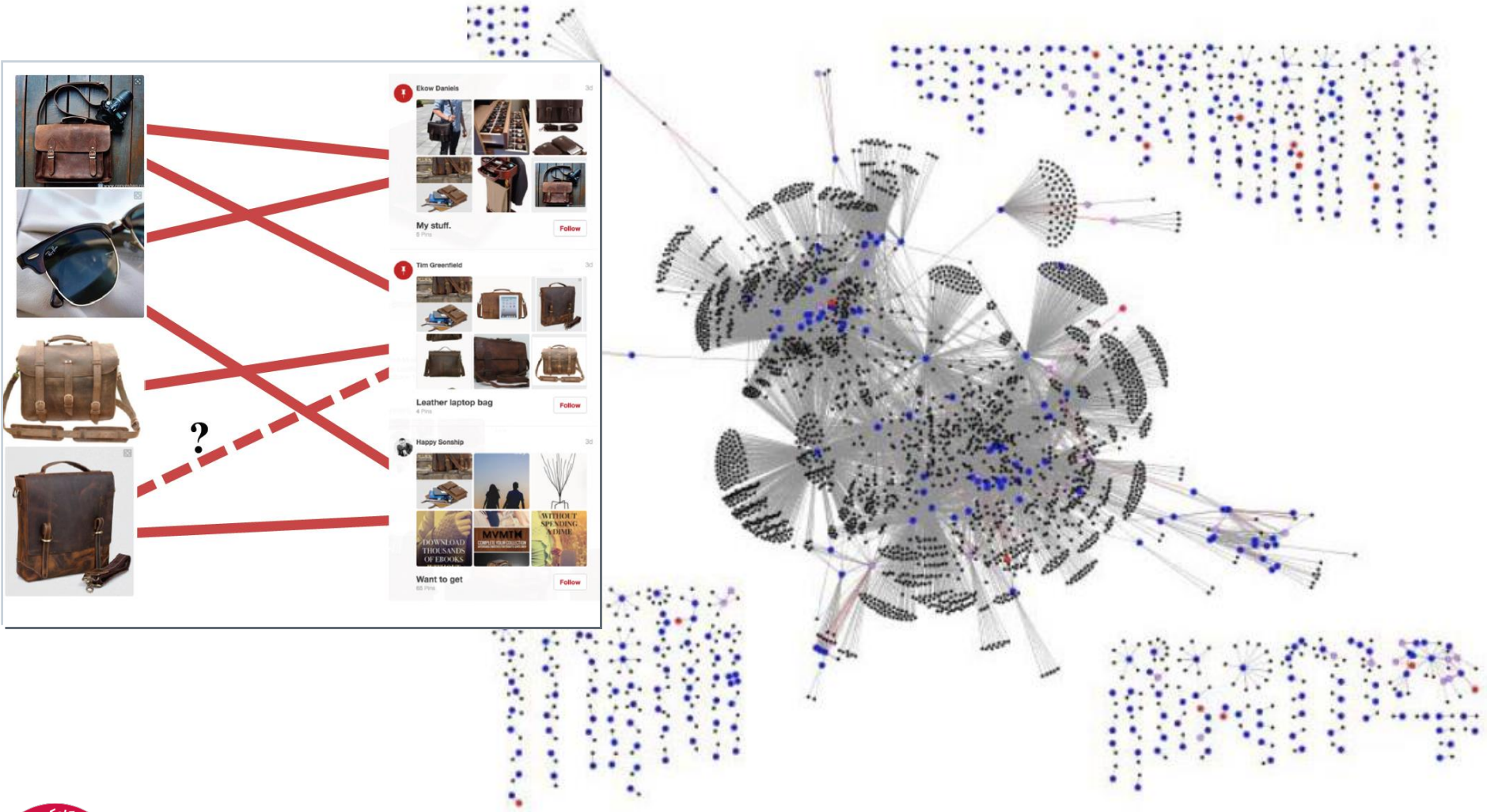


# Links among blogs (2004 presidential election)

---

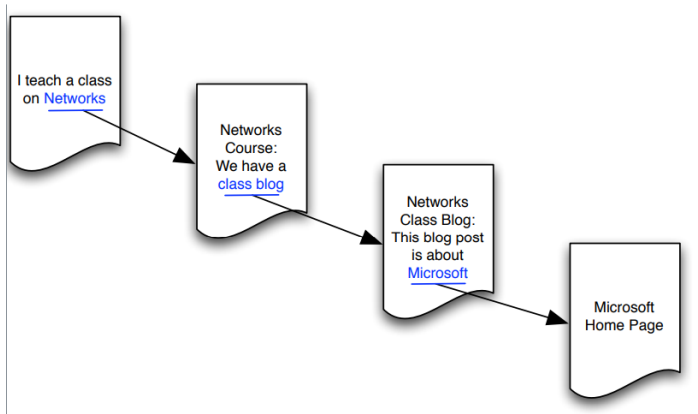


# Product recommendations

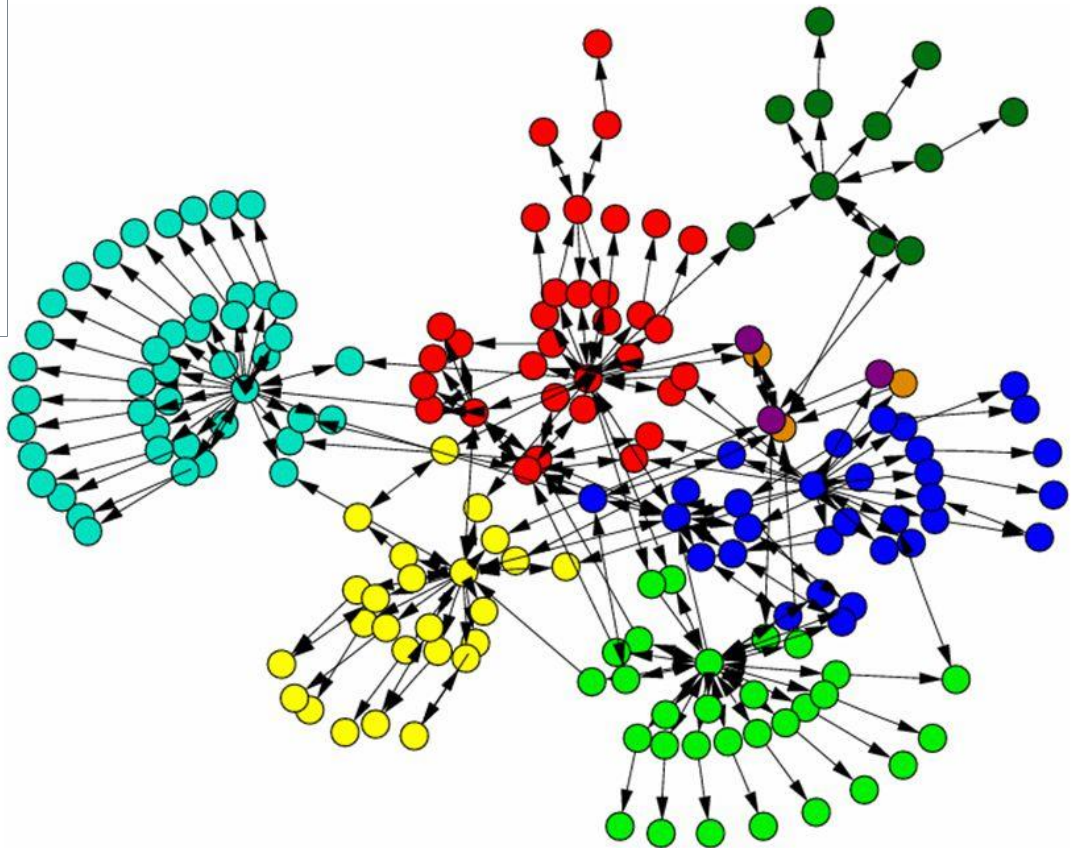


# Webpages

## Webpages connected by hyperlinks



Webpages connected by hyperlinks on the AT&T website circa 1996 visualized by Mark Newman  
Citation networks are similar to the WWW but time-ordered



---

# THE IMPACT OF NETWORK SCIENCE



# Economic Impact



Google  
Market Cap(2010 Jan 1):  
\$189 billion

Cisco Systems  
networking gear Market cap  
(Jan 1, 2019):  
\$112 billion

Facebook  
market cap:  
\$50 billion

[www.bizjournals.com/austin/news/2010/11/15/facebooks...](http://www.bizjournals.com/austin/news/2010/11/15/facebooks...) - Cached

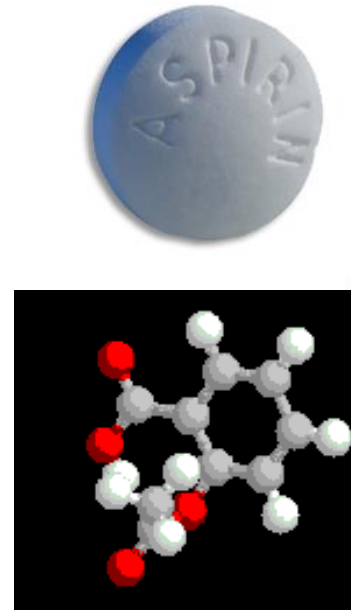
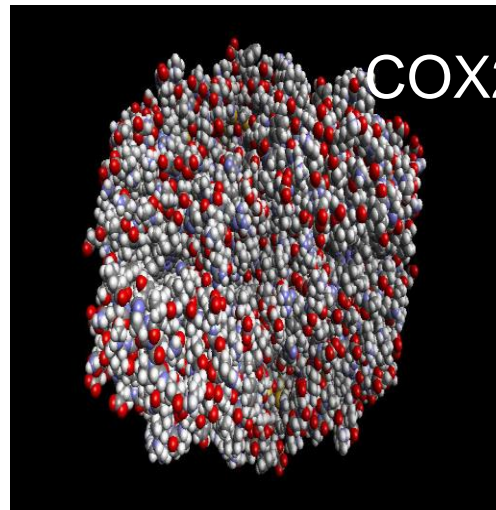
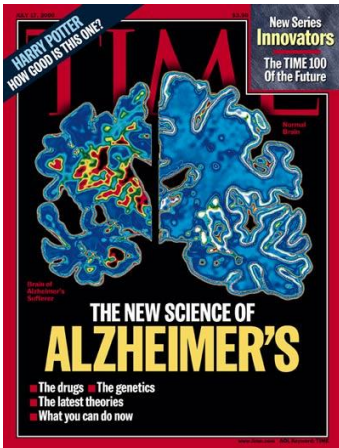
licensed under Attribution-NonCommercial-ShareAlike 2.0 Germany | Ludwig Gatzke | <http://flickr.com/photos/stabilo-boss/>



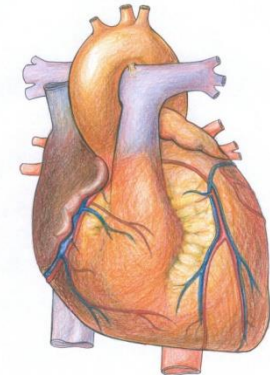
# Drug Design, Metabolic Engineering

**Reduces**

Inflammation  
Fever  
Pain



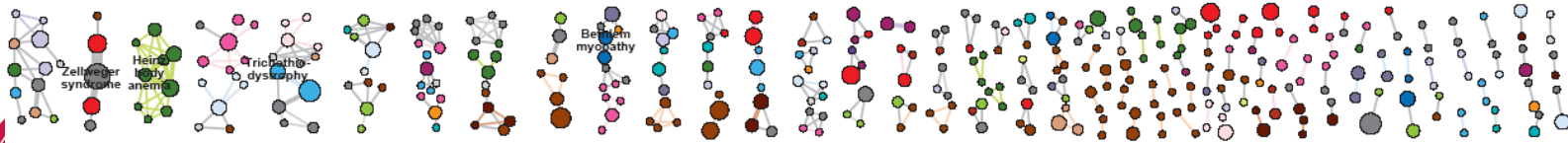
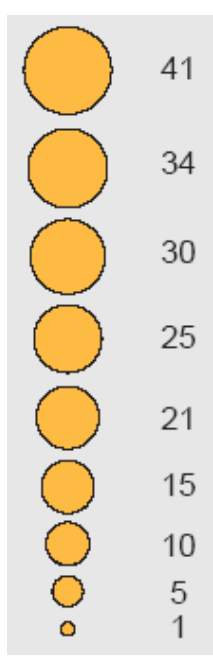
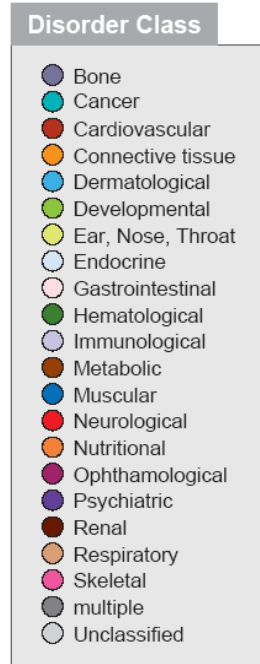
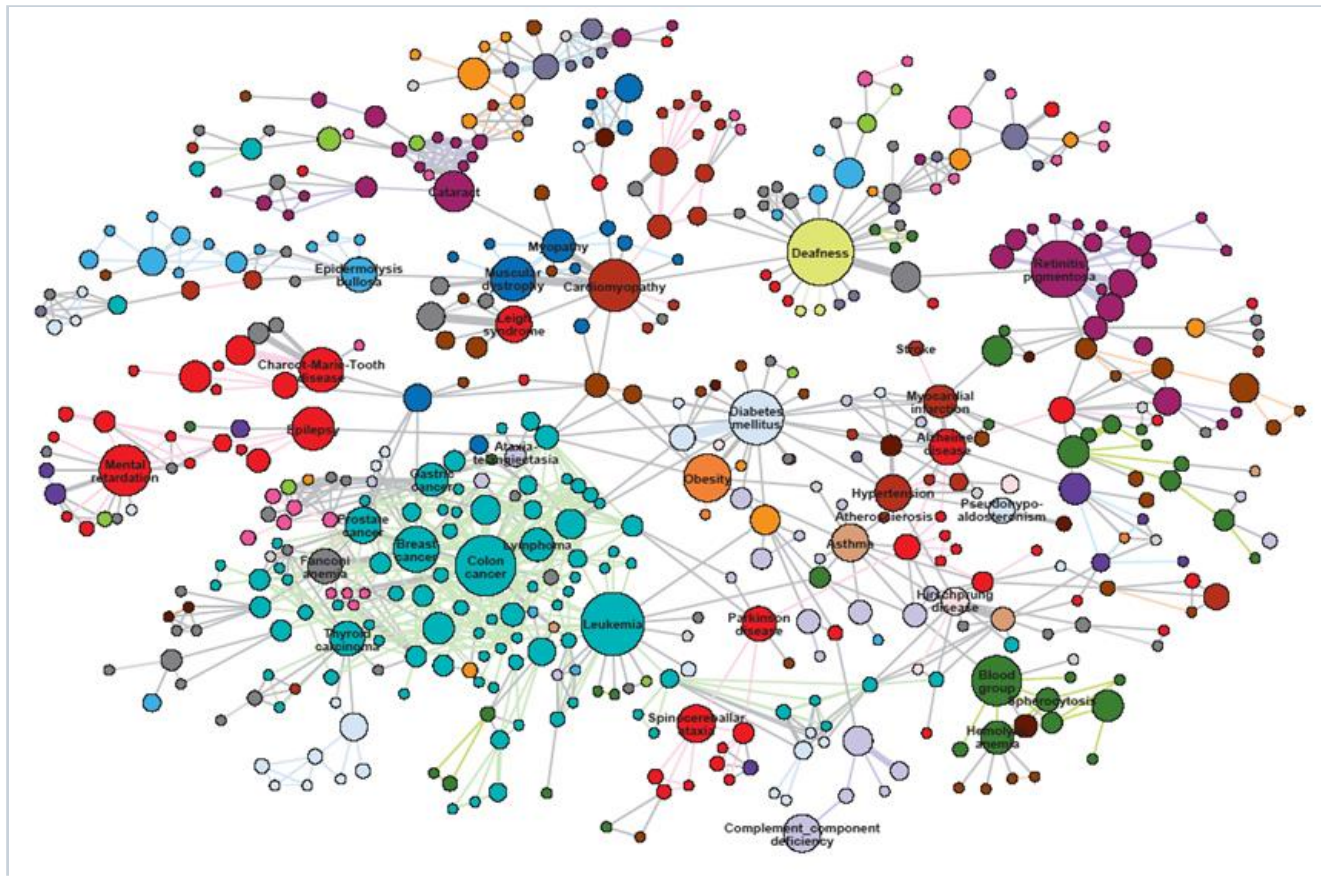
**Prevents**  
Heart attack  
Stroke



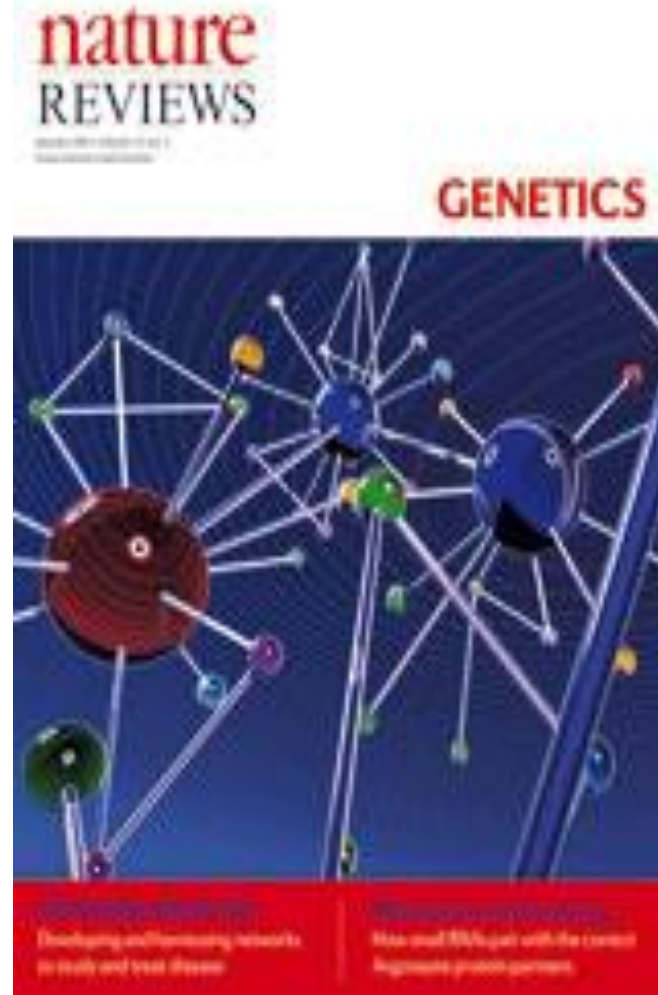
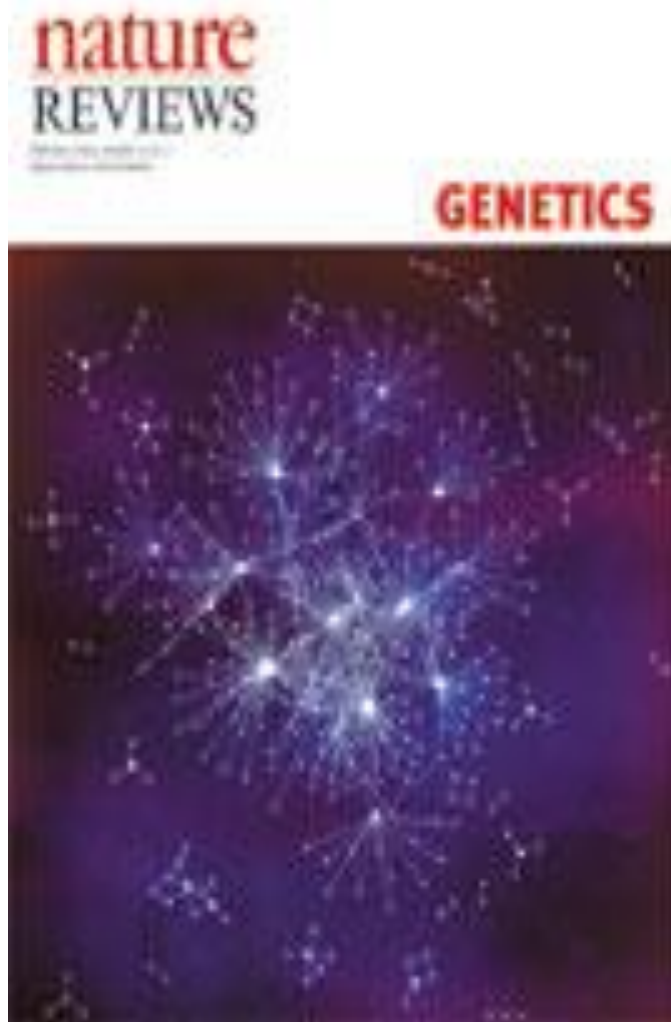
**Reduces the risk of**  
breast cancer  
ovarian cancers  
colorectal cancer

**Causes**  
Bleeding  
Ulcer

# Human Disease Network

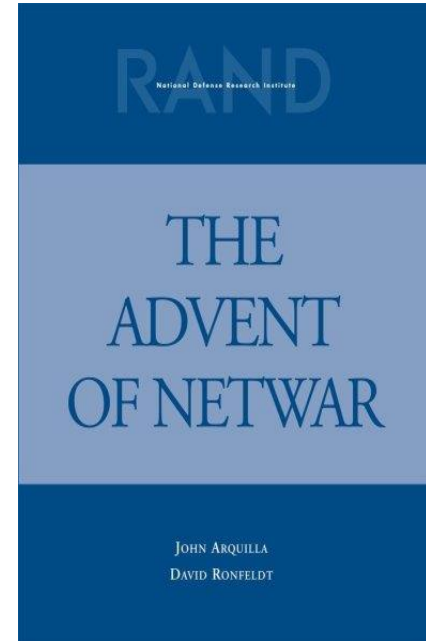
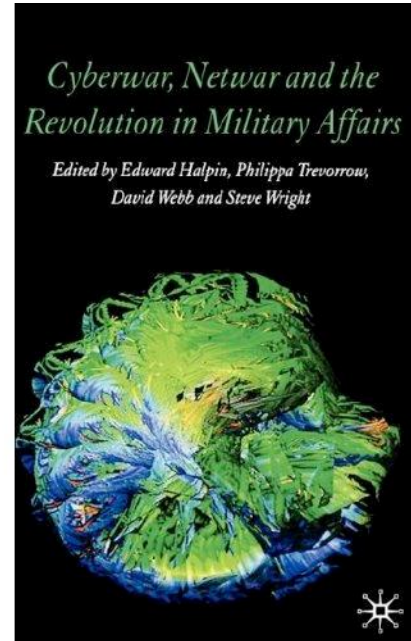


# Network Biology/Network Medicine





# Fighting Terrorism and Military

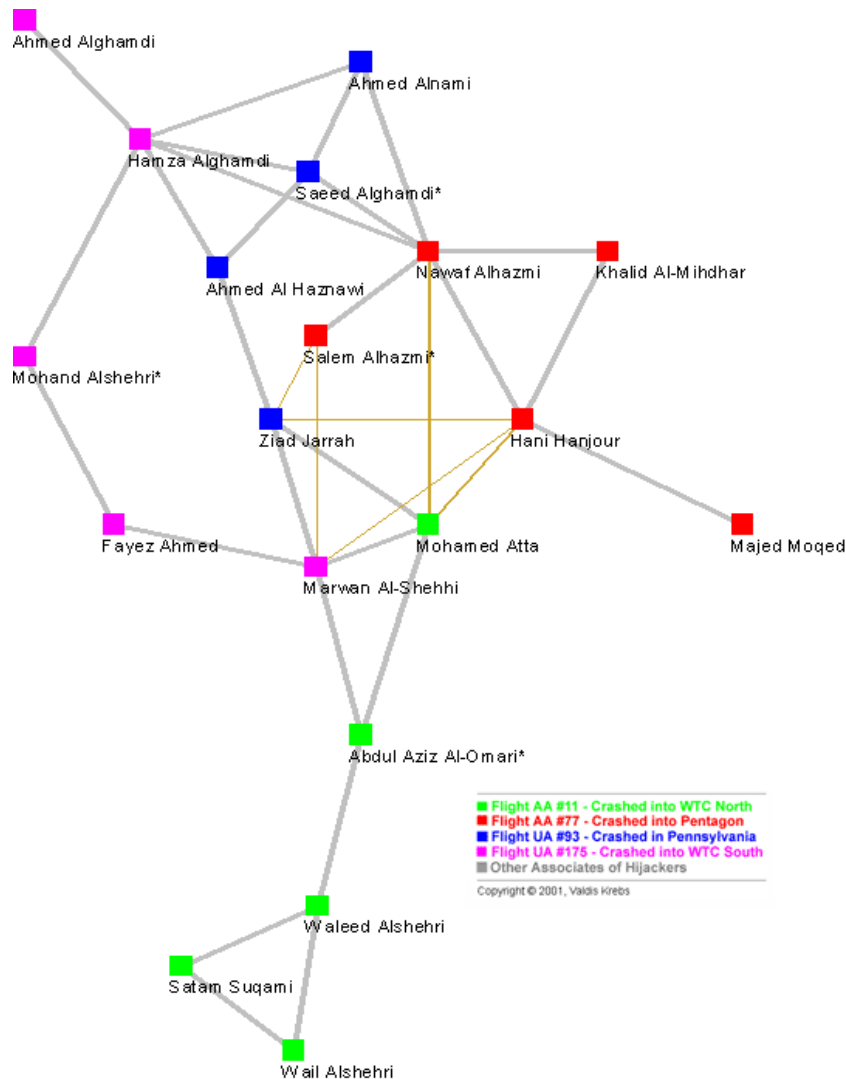


<http://www.slate.com/id/2245232>

Example: the use of social networks to capture Saddam Hussein



# Fighting Terrorism and Military



“Six degrees of Mohammed Atta”

Uncloaking Terrorist Networks, by Valdis Krebs



# Predicting the H1N1 pandemic

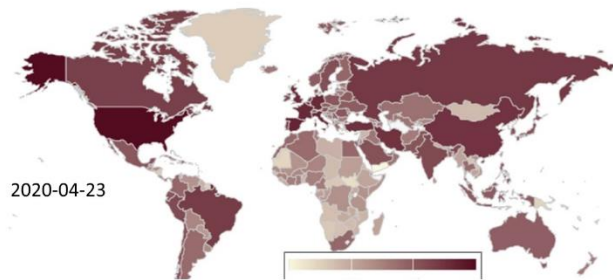
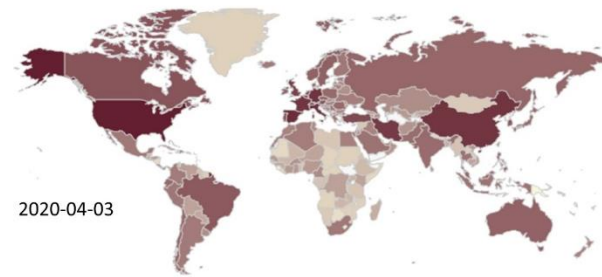
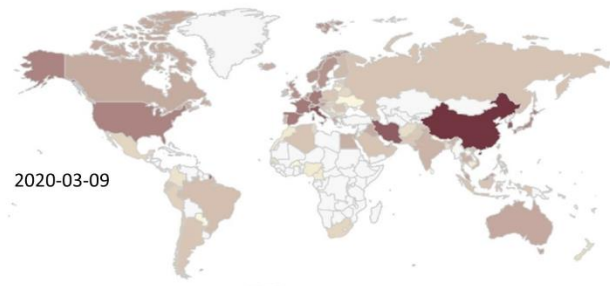
Nov 09 2009



GLEaMviz.org



# COVID 19 Pandemic



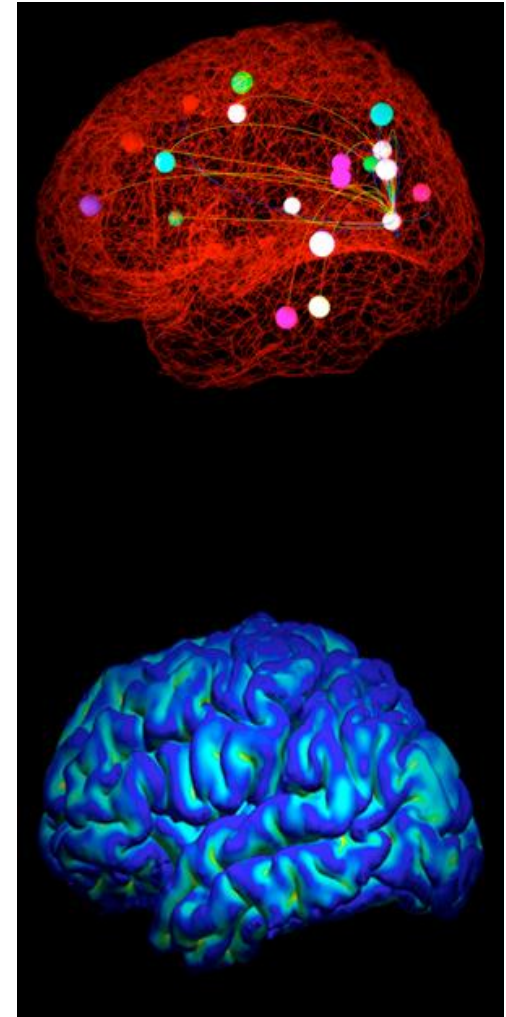
# Brain Research

---

In September 2010 the National Institutes of Health awarded \$40 million to researchers at Harvard, Washington University in St. Louis, the University of Minnesota and UCLA, to develop the technologies that could systematically map out brain circuits.

The Human Connectome Project (HCP) with the ambitious goal to construct a map of the complete structural and functional neural connections in vivo within and across individuals.

<http://www.humanconnectomeproject.org/overview/>



- 
- 1. If you were to understand the spread of diseases, can you do it without networks?**
  - 2. If you were to understand the WWW structure, searchability, etc, hopeless without invoking the Web's topology.**
  - 3. If you want to understand human diseases, it is hopeless without considering the wiring diagram of the cell.**



# Original papers:

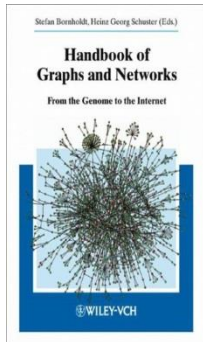
---

- **1998: Watts-Strogatz paper in the most cited Nature publication from 1998; highlighted by ISI as one of the ten most cited papers in physics in the decade after its publication.**
- **1999: Barabasi and Albert paper is the most cited Science paper in 1999; highlighted by ISI as one of the ten most cited papers in physics in the decade after its publication.**
- **2001: Pastor -Satorras and Vespignani is one of the two most cited papers among the papers published in 2001 by Physical Review Letters.**
- **2002: Girvan-Newman is the most cited paper in 2002 Proceedings of the National Academy of Sciences.**

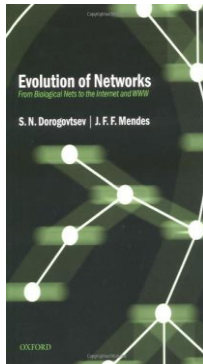




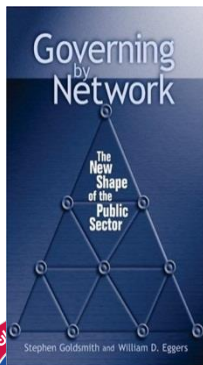
# BOOKS



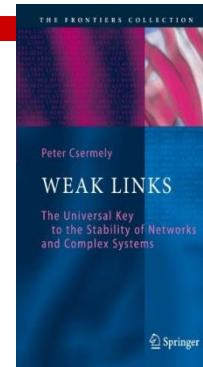
**Handbook of Graphs and Networks: From the Genome to the Internet (Wiley-VCH, 2003).**



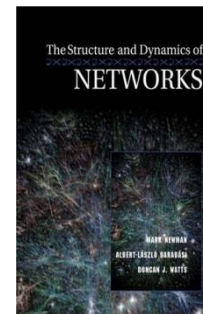
**S. N. Dorogovtsev and J. F. F. Mendes, Evolution of Networks: From Biological Nets to the Internet and WWW (Oxford University Press, 2003).**



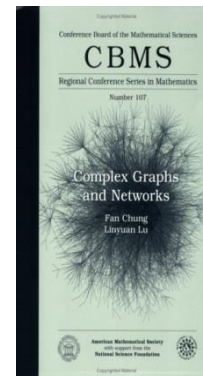
**S. Goldsmith, W. D. Eggers, Governing by Network: The New Shape of the Public Sector (Brookings Institution Press, 2004).**



**P. Csermely, Weak Links: The Universal Key to the Stability of Networks and Complex Systems (The Frontiers Collection) (Springer, 2006), rst edn.**



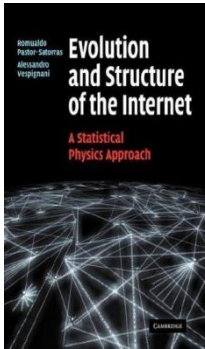
**M. Newman, A.-L. Barabasi, D. J. Watts, The Structure and Dynamics of Networks: (Princeton Studies in Complexity) (Princeton University Press, 2006), rst edn.**



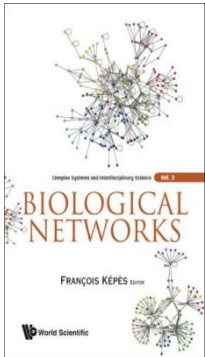
**L. L. F. Chung, Complex Graphs and Networks (CBMS Regional Conference Series in Mathematics) (American Mathematical Society, 2006).**



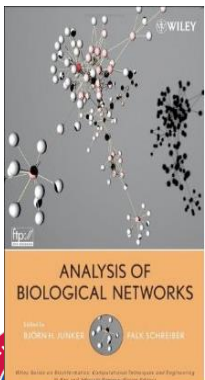
# BOOKS



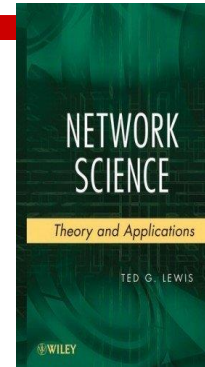
**R. Pastor-Satorras, A. Vespignani, Evolution and Structure of the Internet: A Statistical Physics Approach (Cambridge University Press, 2007), 1st edn.**



**F. Képés, Biological Networks (Complex Systems and Interdisciplinary Science) (World Scientific Publishing Company, 2007), 1st edn.**



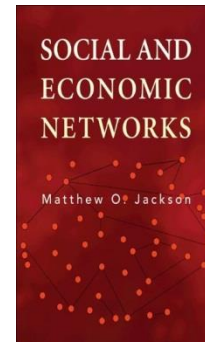
**B. H. Junker, F. Schreiber, Analysis of Biological Networks (Wiley Series in Bioinformatics) (Wiley-Interscience, 2008).**



**T. G. Lewis, Network Science: Theory and Applications (Wiley, 2009).**



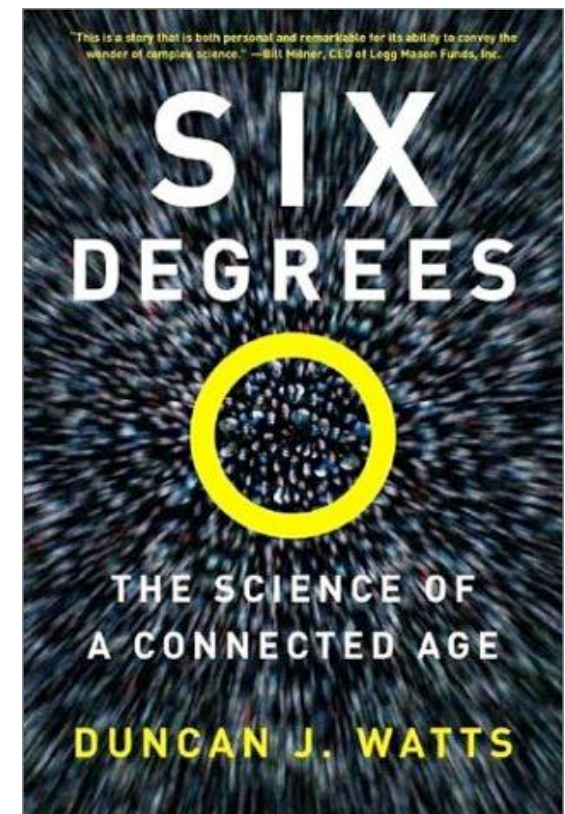
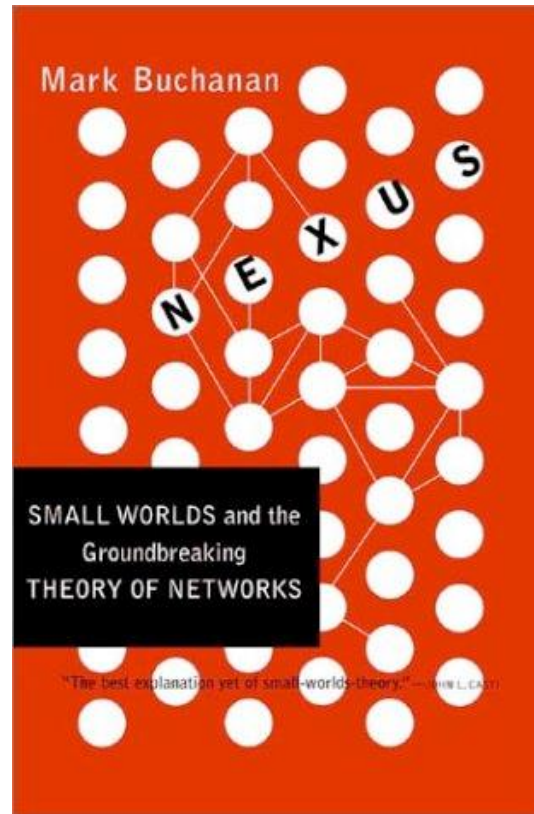
**E. Ben Naim, H. Frauenfelder, Z. Torotzai, Complex Networks (Lecture Notes in Physics) (Springer, 2010), 1st edn.**



**M. O. Jackson, Social and Economic Networks (Princeton University Press, 2010).**

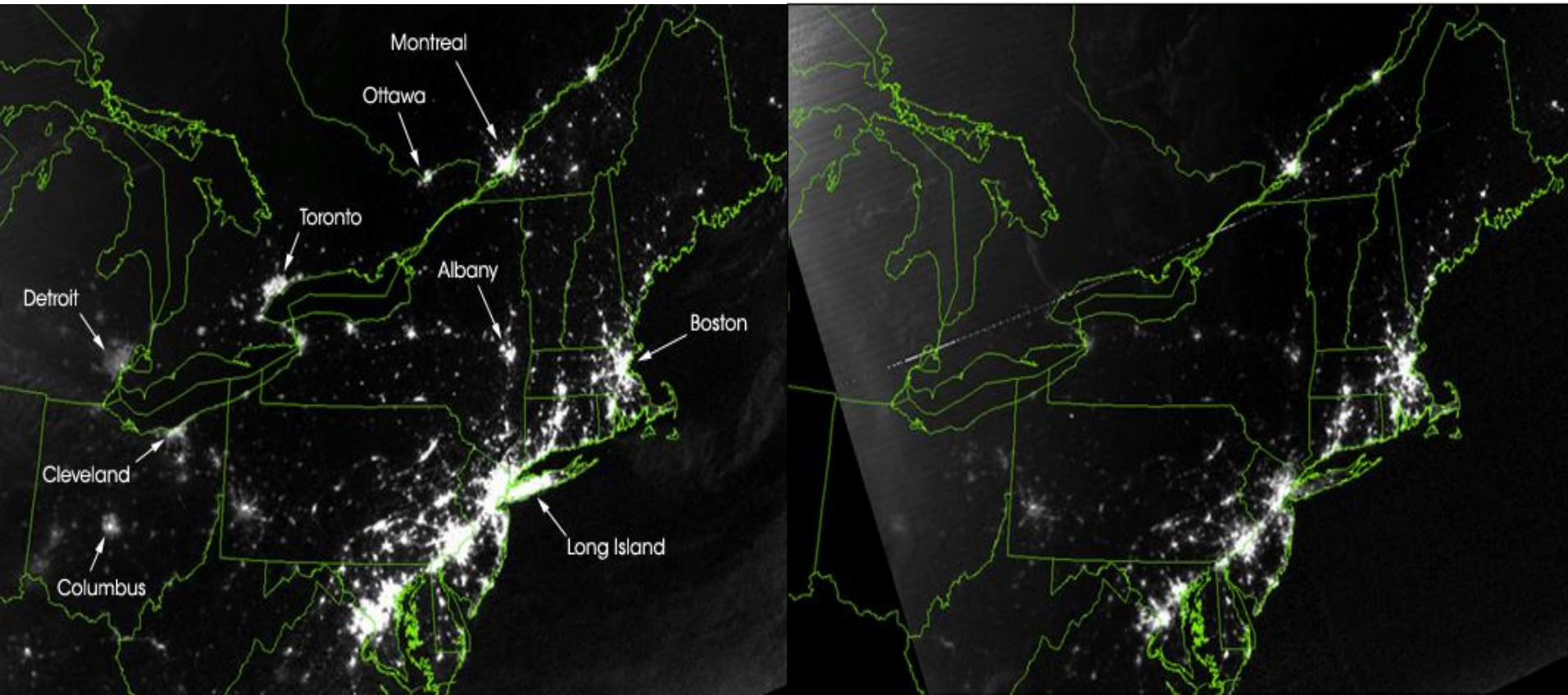


# General Audience



# A Simple Story(2): August 15, 2003 blackout

---



August 14, 2003: 9:29pm EDT  
20 hours before

August 15, 2003: 9:14pm EDT  
7 hours after



# A Simple Story(2): August 15, 2003 blackout

---

**This reveals two important themes of this class:**

- We must understand how network structure affects the robustness of a system
- Develop quantitative tools to assess the interplay between network structure and the dynamical processes on the networks, and their impact on failures



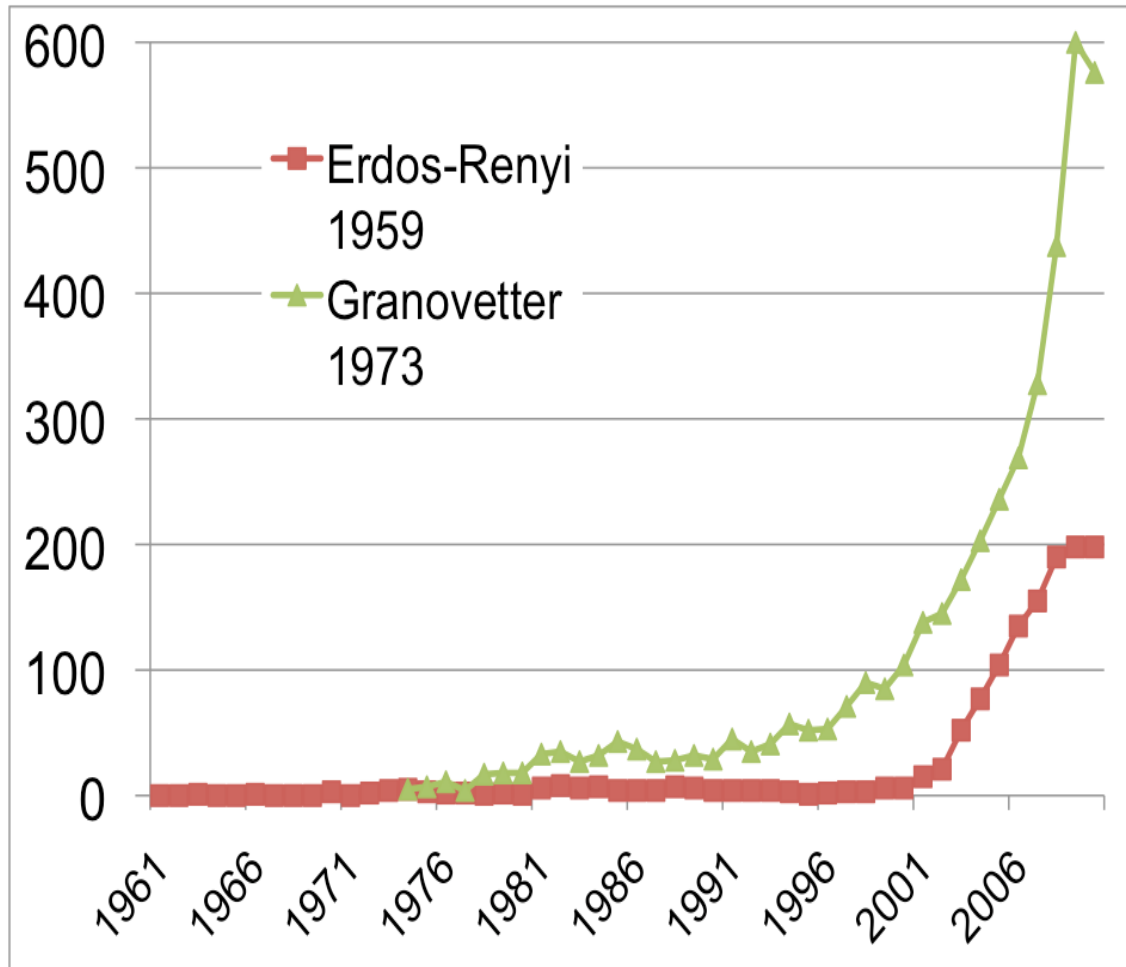
# The History of Network Analysis

---

- **Graph theory: 1735, Euler**
- **Social Network Research: 1930s, Moreno**
- **Communication networks/internet: 1960s**
- **Ecological Networks: May, 1979.**



# The History of Network Analysis



# The Emergence of Network Maps

---

- Movie Actor Network, 1998
- World Wide Web, 1999
- C-elegans neural wiring diagram 1990
- Citation Network, 1998
- Metabolic Network, 2000;
- PPI network, 2001





# Reasoning about networks

---

- How do we reason about networks?
  - Empirical: Study network data to find organizational principles
  - Mathematical models: Probabilistic, graph theory
  - Algorithms: analyzing graphs
- What do we hope to achieve from studying networks?
  - Patterns and statistical **properties** of network data
  - **Design principles** and **models**
  - Understand why networks are organized the way they are
    - Predict behavior of networked systems



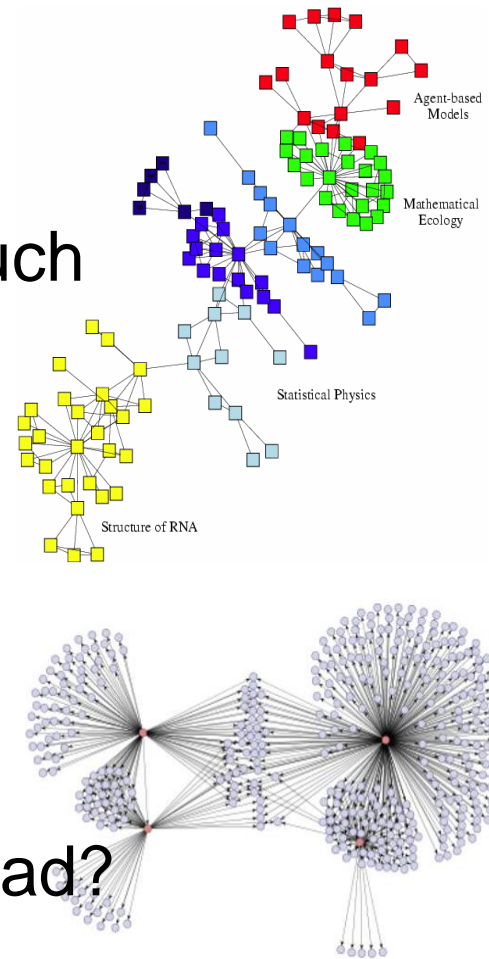
# What do we study in networks?

- Structure and evolution

- What is the structure of a network?
- Why and how did it become to have such structure?

- Processes and dynamics

- Networks provide a “skeleton” for spreading of information, behavior, diseases
- How do information and diseases spread?



# Why to analyze networks?

---

- **Predict the type/color of a given node**  
Node classification
- **Predict whether two nodes are linked**  
Link prediction
- **Identify densely linked clusters of nodes**  
Community detection
- **Measure similarity of two nodes/networks**  
Network similarity



# Networks in complex systems

---

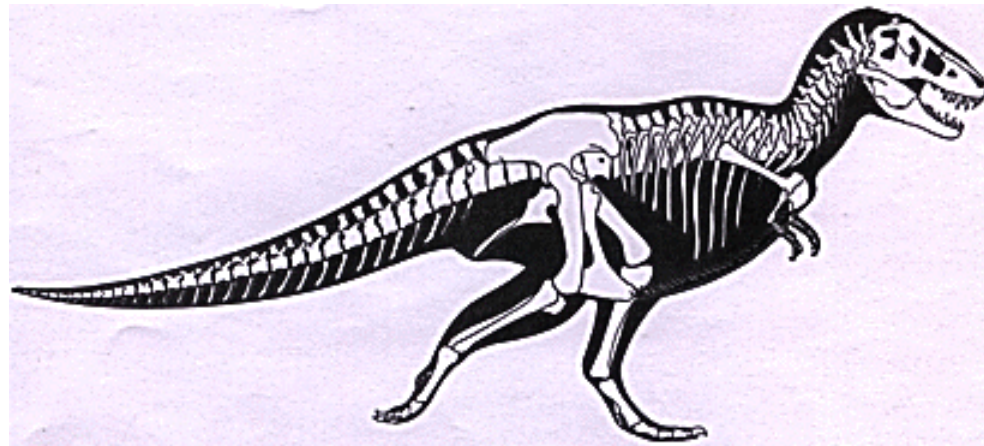
- **Complex systems**
  - Large number of components interacting with each other
  - All components and/or interactions are different from each other
  - Paradigms:
    - $10^4$  types of proteins in an organism,
    - $10^6$  routers in the Internet
    - $10^9$  web pages in the WWW
    - $10^{11}$  neurons in a human brain
- The simplest property:
  - who interacts with whom?
    - can be visualized as a network
- **Complex networks** are just a backbone for complex dynamical systems



# Why study the topology of Complex Networks?

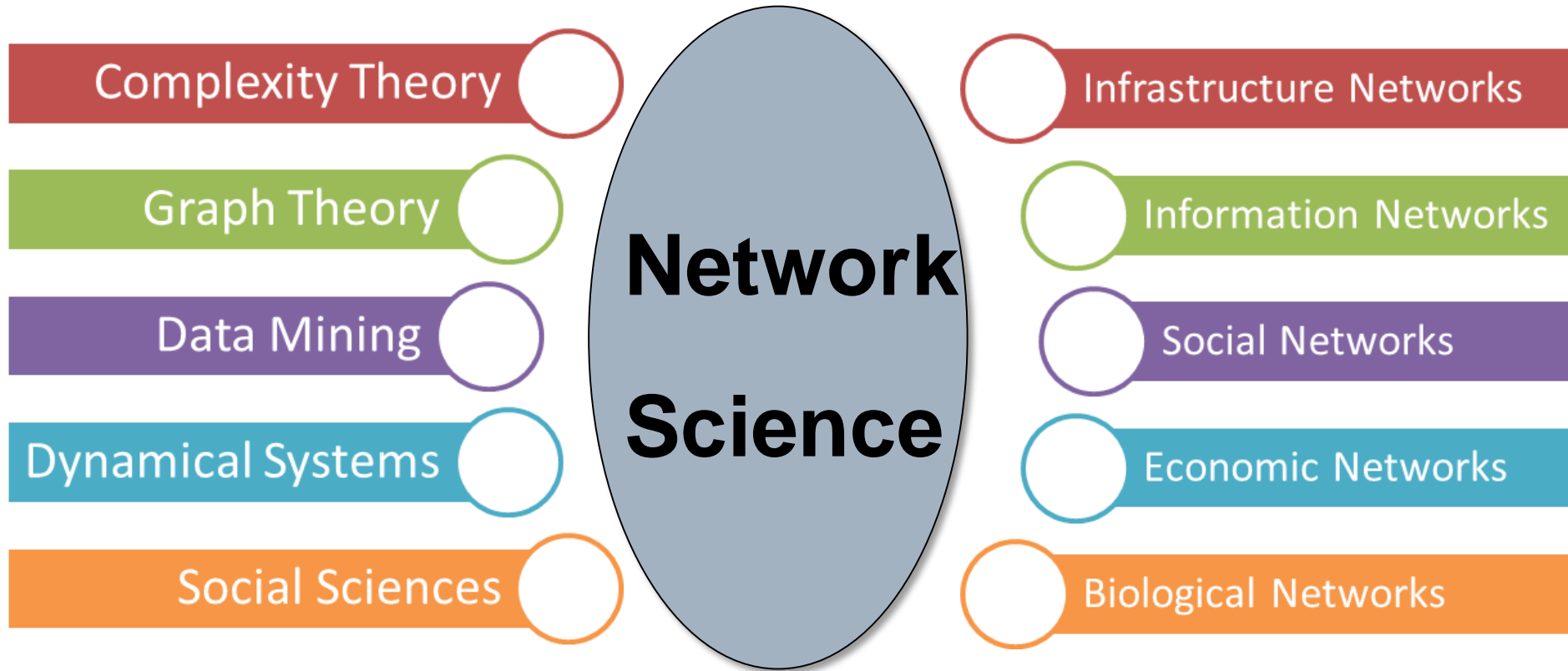
---

- Lots of easily available data
- Large networks may contain information about basic design principles and/or evolutionary history of the complex system
- This is similar to paleontology:
  - learning about an animal from its backbone



# A Multidisciplinary Research Field

---



# Network Questions: Structural

---

1. How many connections does the average node have?
2. Are some nodes more connected than others?
3. Is the entire network connected?
4. On average, how many links are there between nodes?
5. Are there clusters or groupings within which the connections are particularly strong?
6. What is the best way to characterize a complex network?
7. How can we tell if two networks are “different”?
8. Are there useful ways of classifying or categorizing networks?



# Network Questions: Communities

---

1. Are there clusters or groupings within which the connections are particularly strong?
2. What is the best way to discover communities, especially in large networks?
3. How can we tell if these communities are statistically significant?
4. What do these clusters tell us in specific applications?





# Network Questions: Dynamics of

---

1. How can we model the growth of networks?
2. What are the important features of networks that our models should capture?
3. Are there “universal” models of network growth? What details matter and what details don't?
4. To what extent are these models appropriate null models for statistical inference?
5. What's the deal with power laws, anyway?



# Network Questions: Dynamics on

---

1. How do diseases/computer viruses/innovations/rumors/revolutions propagate on networks?
2. What properties of networks are relevant to the answer of the above question?
3. If you wanted to prevent (or encourage) spread of something on a network, what should you do?
4. What types of networks are robust to random attack or failure?
5. What types of networks are robust to directed attack?
6. How are dynamics of and dynamics on coupled?



# Network Questions: Algorithms

---

1. What types of networks are searchable or navigable?
2. What are good ways to visualize complex networks?
3. How does google page rank work?
4. If the Internet were to double in size, would it still work?



# Network Questions: Algorithms

---

There are also many domain-specific questions:

1. Are networks a sensible way to think about gene regulation or protein interactions or food webs?
2. What can social networks tell us about how people interact and form communities and make friends and enemies?
3. Lots and lots of other theoretical and methodological questions...
4. What else can be viewed as a network? Many applications await.



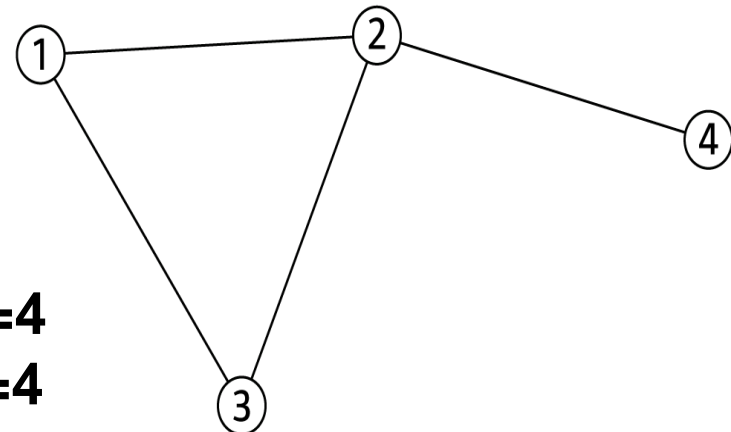
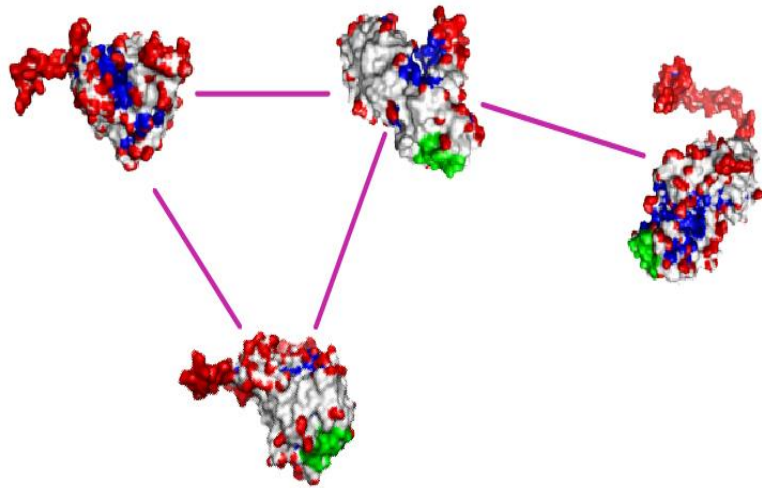
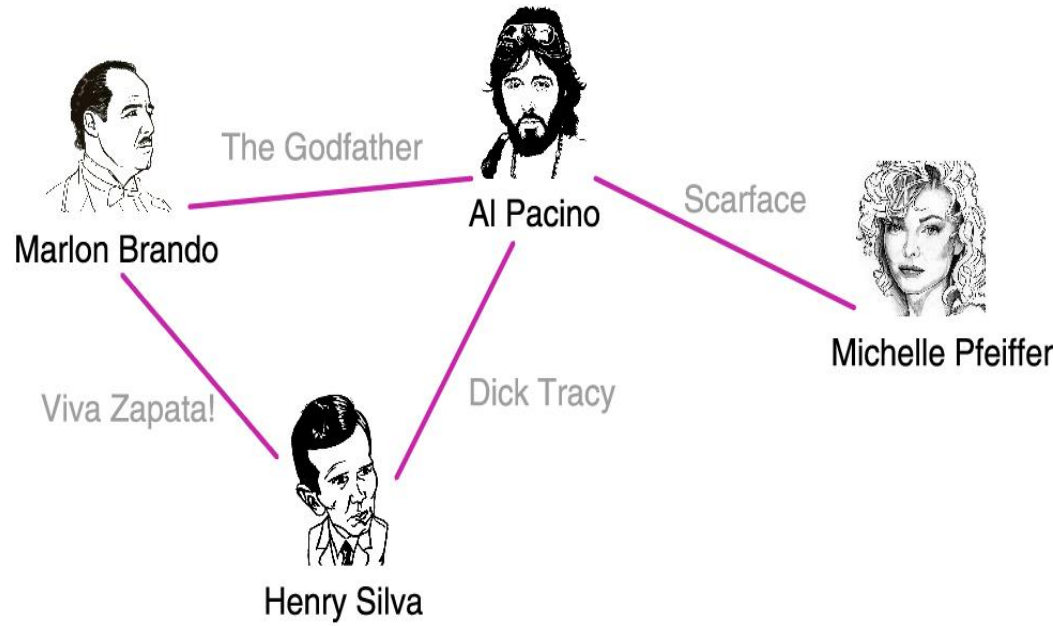
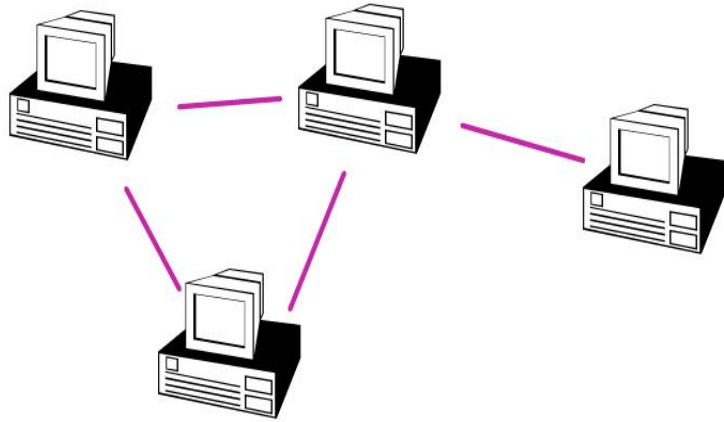
# Network Questions: Outlook

---

- Advances in available data, computing speed, and algorithms have made it possible to apply network analysis to a vast and growing number of phenomena.
- This means that there is lots of exciting, novel work being done
- This work is a mixture of awesome, exploratory, misleading, irrelevant, relevant, fascinating, ground-breaking, important, and just plain wrong
- It is relatively easy to fool oneself into seeing things that aren't there when analyzing networks.
- This is the case with almost anything, not just networks
- For networks, how can we be more careful and scientific, and not just descriptive and empirical?



# A Common Language



**N=4**  
**L=4**



# A Common Language

---

| <b>Network</b>  | <b>Nodes</b>                     | <b>Edges</b>                           |
|-----------------|----------------------------------|--|
| biochemical     | molecules                        | chemical reactions                     |
| neural          | neurons                          | synaptic connections                   |
| epidemiological | healthy, infected individuals    | infectious contacts                    |
| world wide web  | web pages                        | hyperlinks                             |
| trophic         | predators, prey                  | predation interactions                 |
| power grid      | electrical generators, end users | power lines, substations, transformers |
| collaborative   | scientists, engineers            | collaborations                         |
| social          | people                           | friendships                            |
| internet        | computers                        | routers, ethernet cables               |



# Property of Friendship

---

- **Six Degrees of Separation**

## Milgram (1967)

### The experiment:

- Random people from Nebraska were to send a letter (via intermediaries) to a stock broker in Boston.
- Could only send to someone with whom they know.



**Stanley Milgram (1933-1984)**



# Small world experiment

---



Milgram's experiment (1960's):

- Given a target individual and a particular property, pass the message to a person you correspond with who is "closest" to the target.

"Six degrees of separation"

# Small World Network

---

“A **small world network** is a type of mathematical graph in which most nodes are not neighbors of one another, but most nodes can be reached from every other by a **small** number of hops or steps.” - Wikipedia



# Some Famous Researchers



Mark Newman, 146, 55  
• University of Michigan



Steven H. Strogatz, 107, 29  
• Cornell University



Albert Laszlo Barabasi, 198, 72  
• Harvard University



Duncan Watts, 43, 25  
• Yahoo Research Labs



Jon Kleinberg, 150, 40  
• Cornell University



Alex Arenas, 92, 27  
• University of Zaragoza



Réka Albert, 78, 31  
• Pennsylvania State University



Jure Leskovec, 54, 19  
• Stanford University



Santo Fortunato, 65, 23  
• Institute for Scientific Interchange Foundation



David Kempe, 53, 17  
• University of Southern California

# Wrap up

---

- networks are everywhere and can be used to describe many, many systems
- Network science research studies physical, biological, social, artificial, engineered, and other phenomena that arise in systems made of a large number of mutually interacting components whose macroscopic properties are not easy to understand or explain
- by modeling networks we can start to understand their properties and the implications those properties have for processes occurring on the network



# Final Word



A clear blue sky with several fluffy white clouds scattered across it. The clouds are of varying sizes and are positioned mostly in the upper and middle sections of the frame. The word "Questions" is written in a large, white, sans-serif font in the bottom right corner.

**Questions**